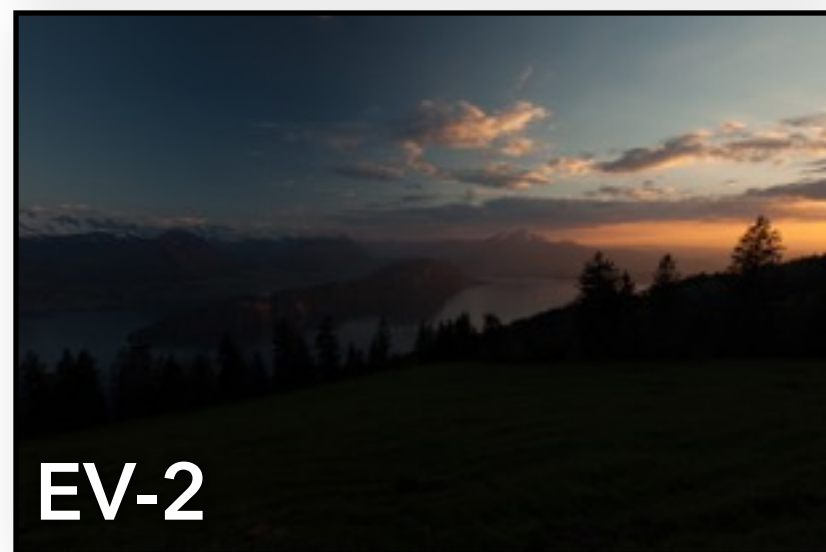


# HIGH-DYNAMIC-RANGE PHOTOGRAPHY + TONE MAPPING II



# Last time

---

The dynamic range challenge

Applications of HDR photography

Capturing HDR images

Merging bracketed exposures

Tone mapping

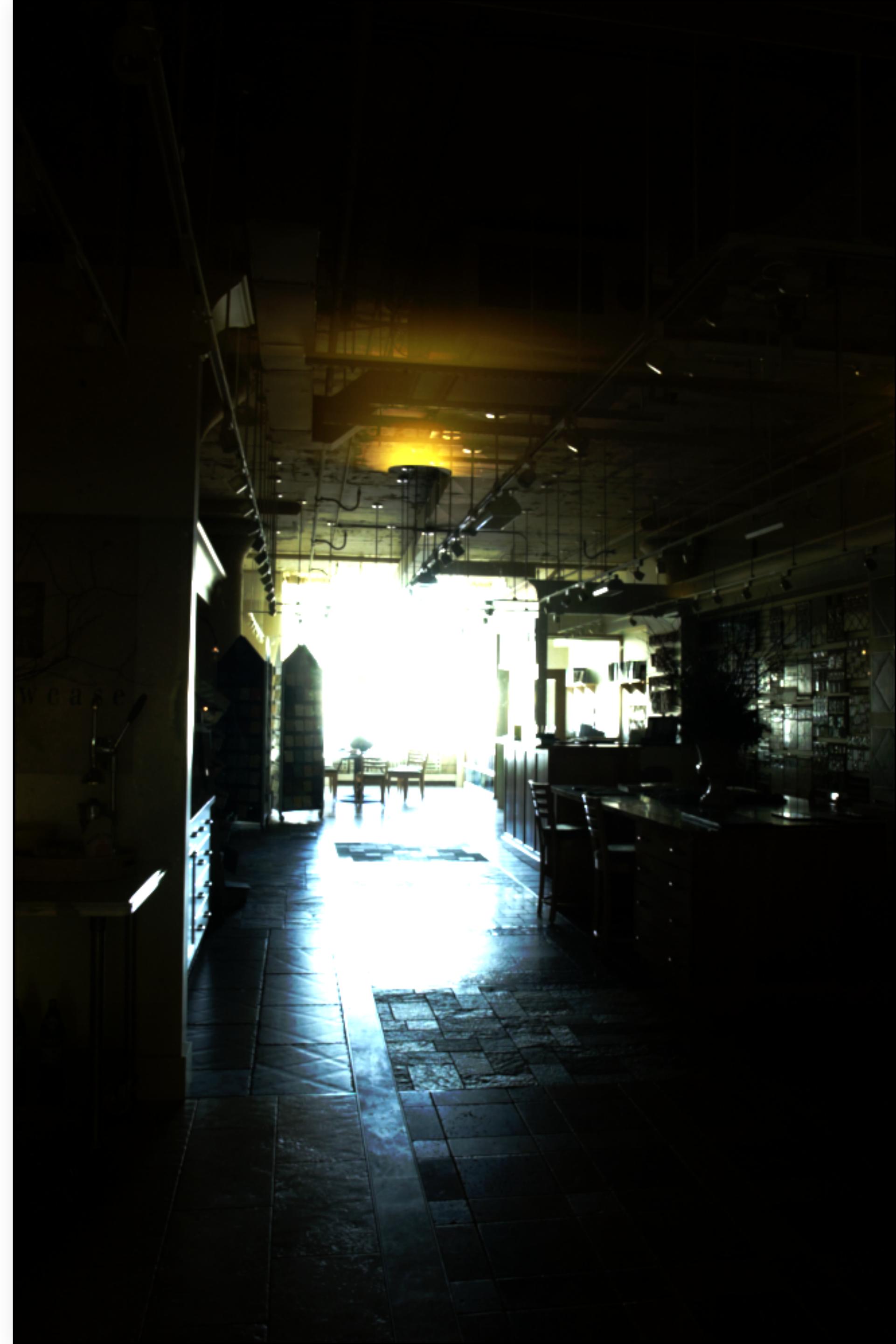
- global operators
- local operators

# Examples

Inside is too dark  
Outside is too bright

Sun overexposed

Foreground too dark



# Without HDR & tone mapping



**With** HDR & tone mapping



# HDR today

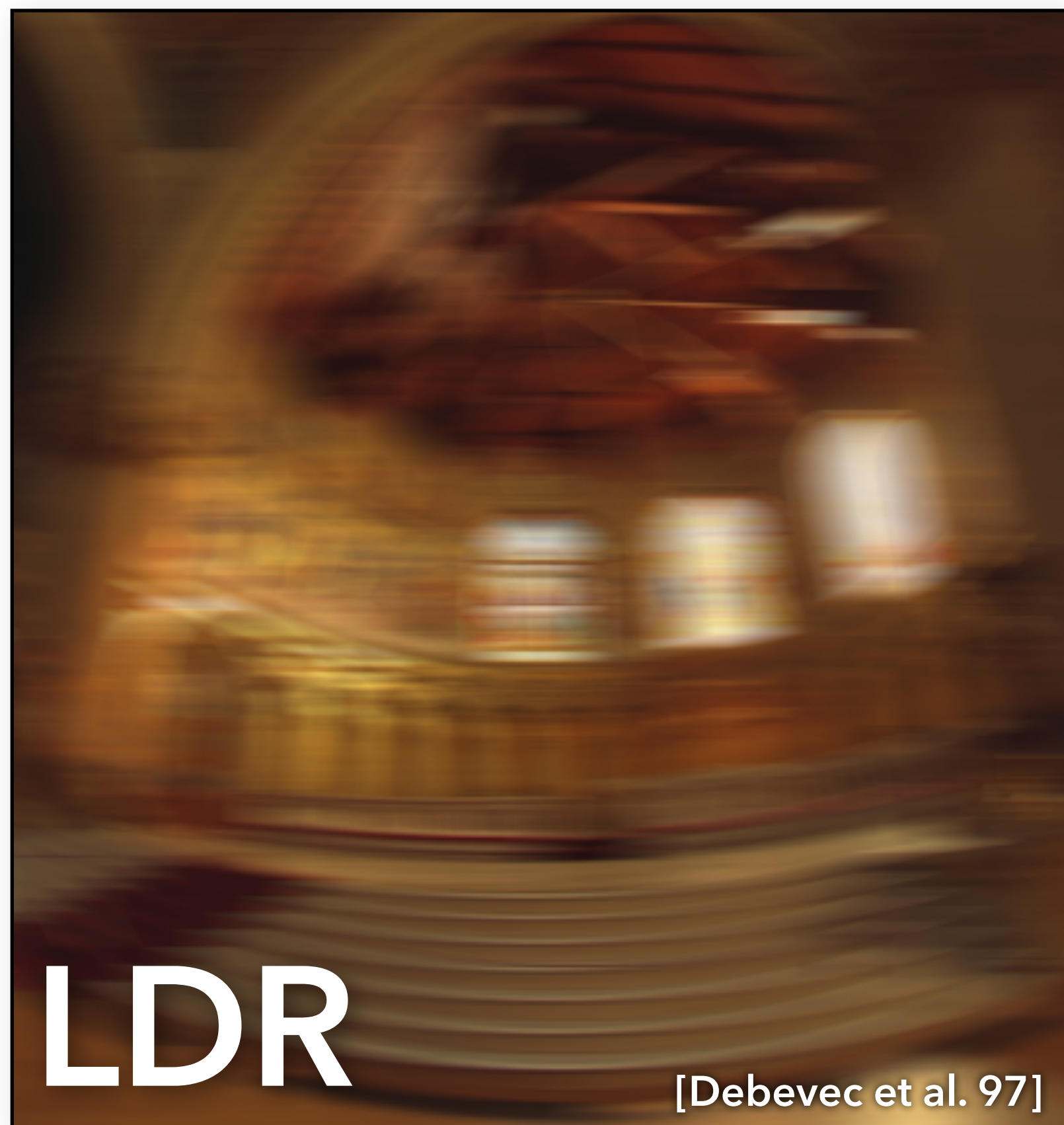
HDR Off

HDR On



# Application: Motion blur

Simulated Motion



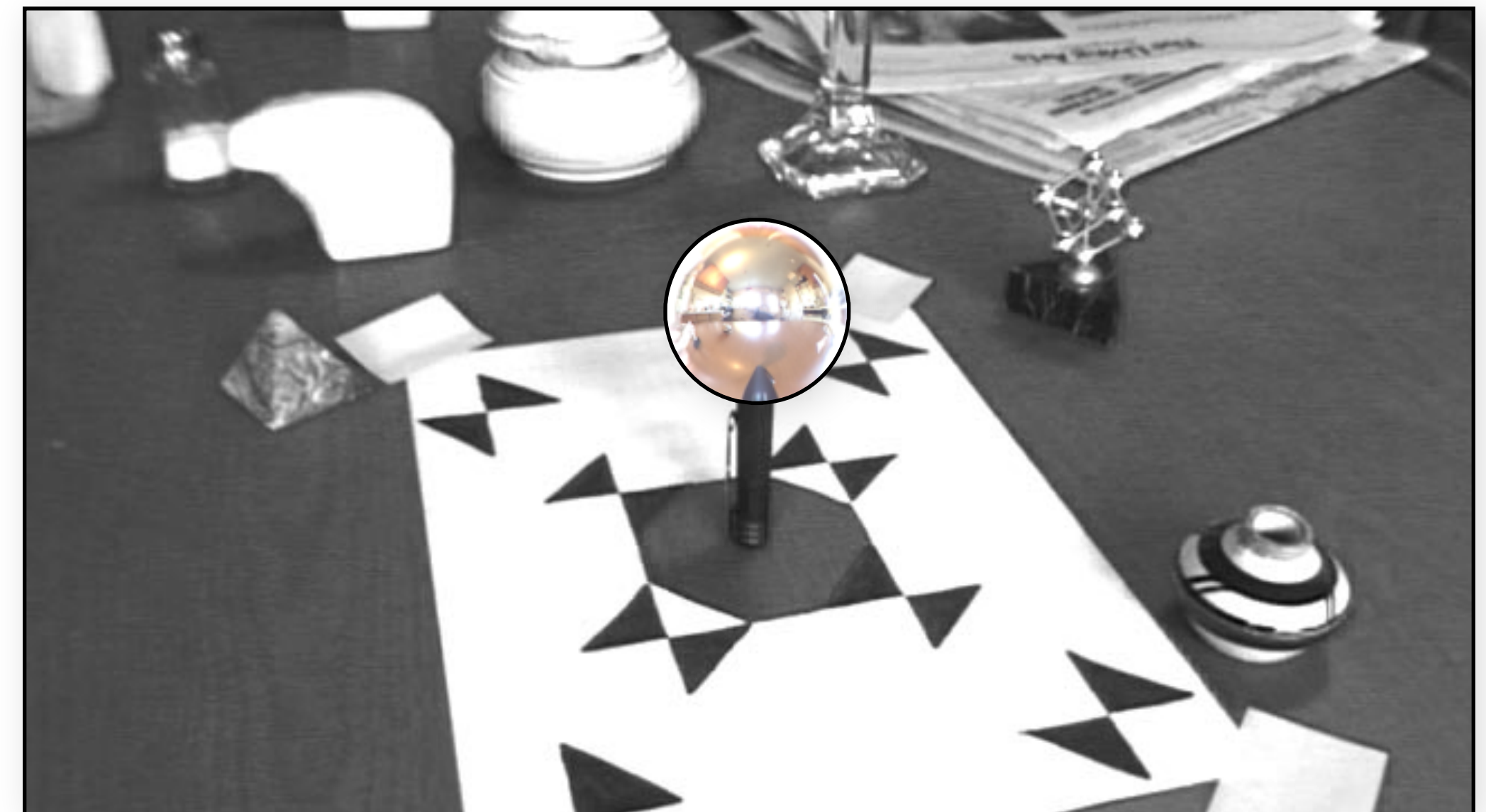
Simulated Motion Blur



Actual Motion blur



# Application: Inserting Synthetic Objects



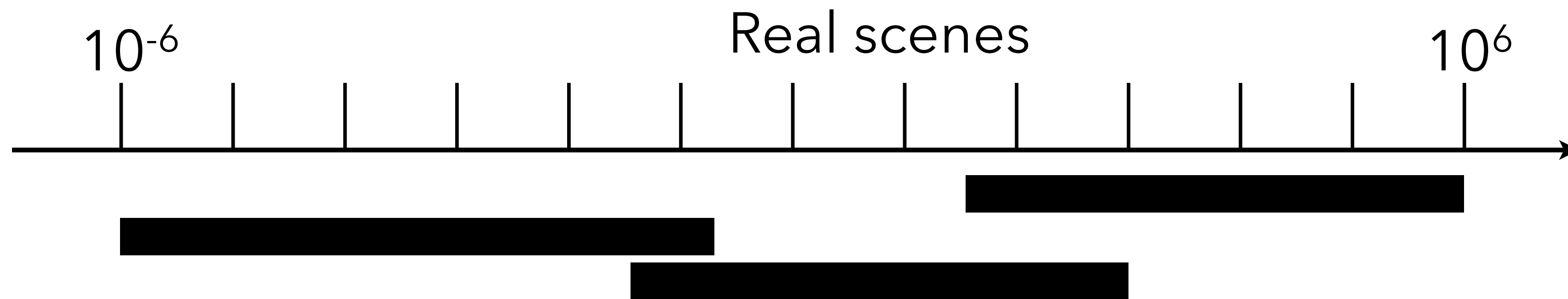


# Application: Inserting Synthetic Objects

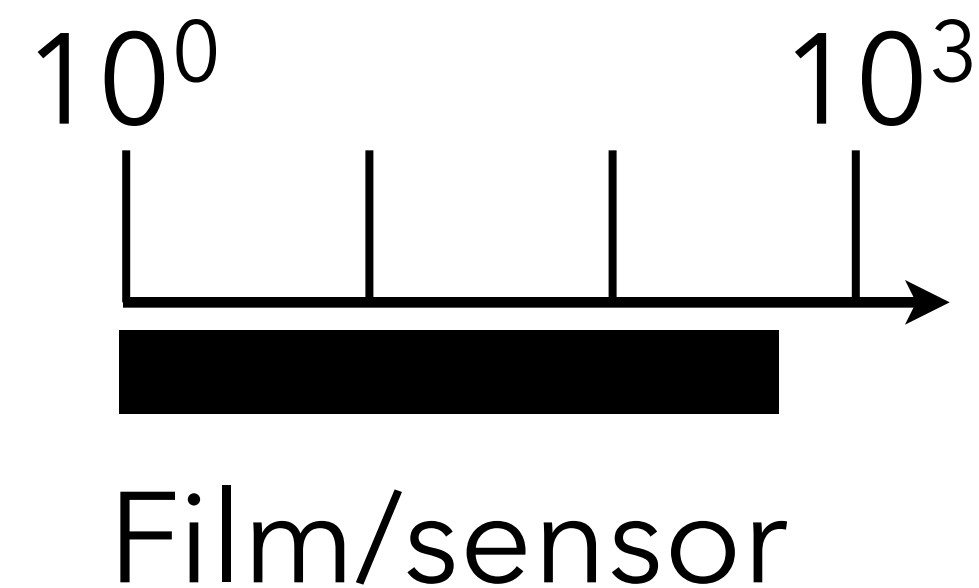


# Problem 1: Record the information

The range of illumination levels that we encounter is 10-12 orders of magnitude

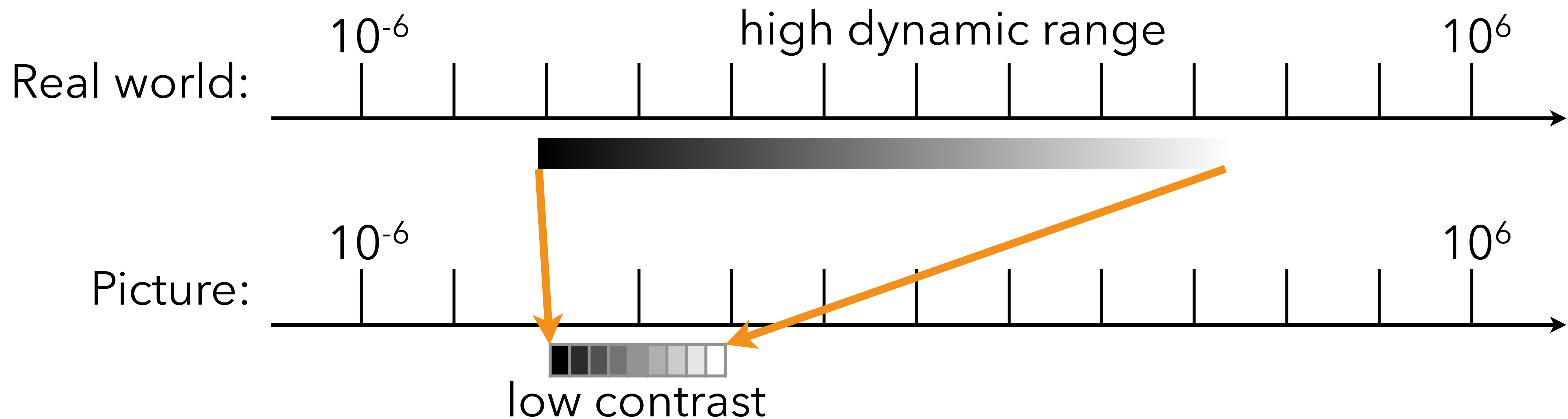


Film/sensors can record 2-3 orders of magnitude



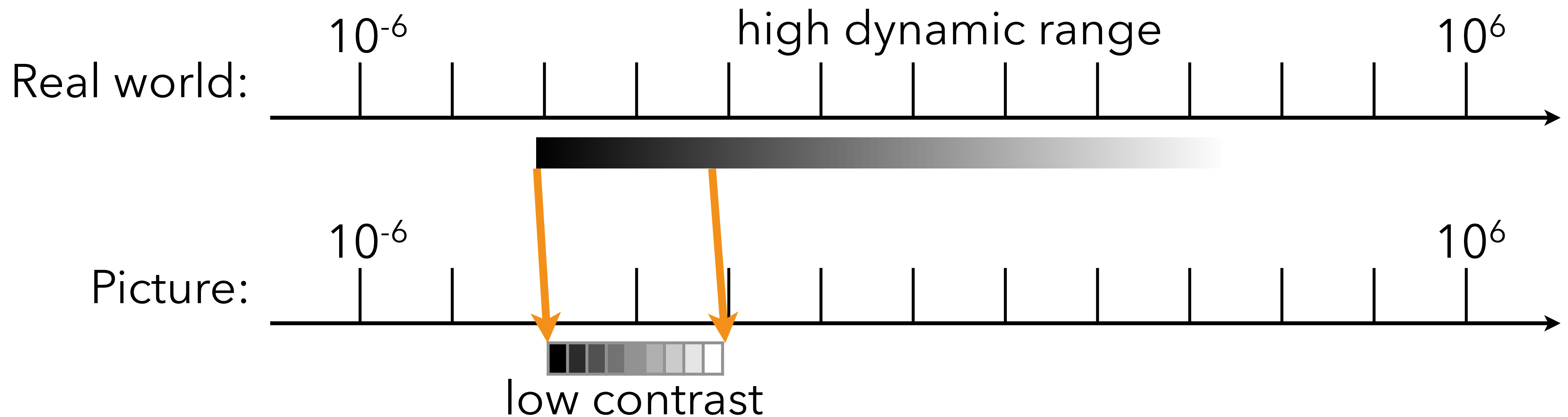
# Multiple exposure photography

Sequentially measure all segments of the range



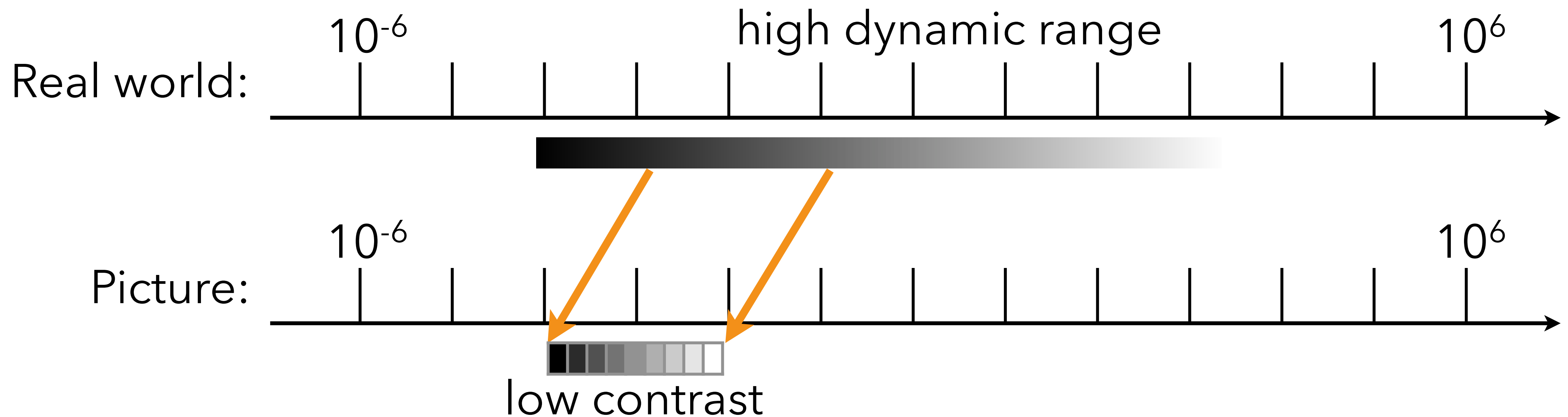
# Multiple exposure photography

Sequentially measure all segments of the range



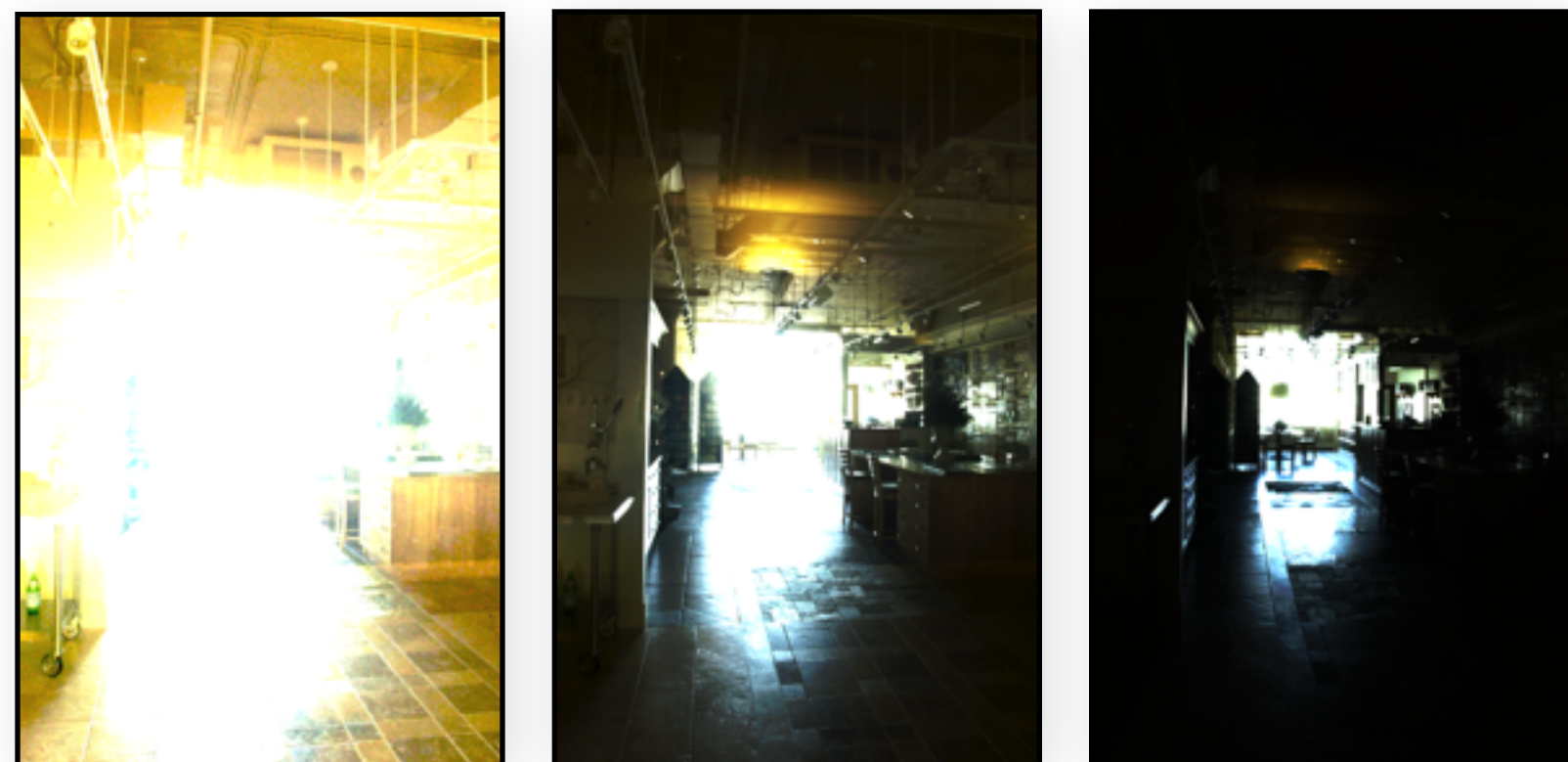
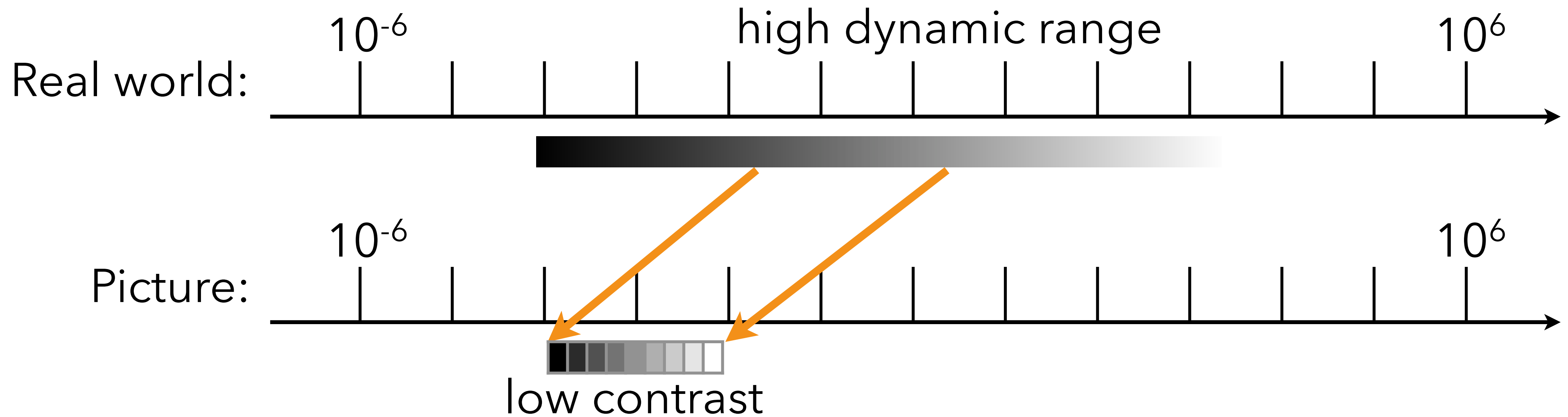
# Multiple exposure photography

Sequentially measure all segments of the range



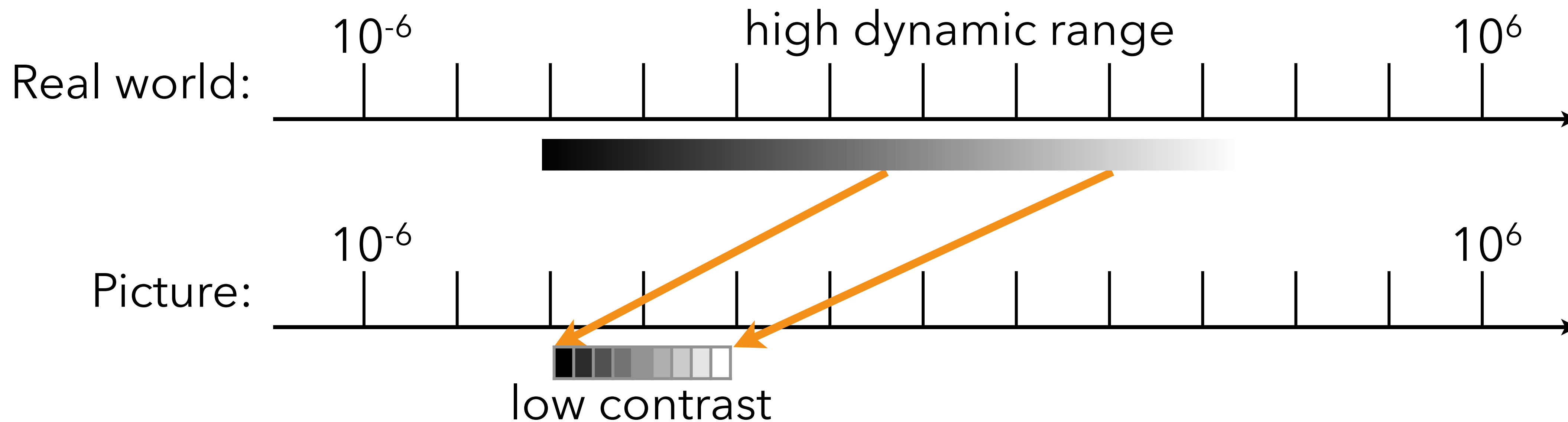
# Multiple exposure photography

Sequentially measure all segments of the range



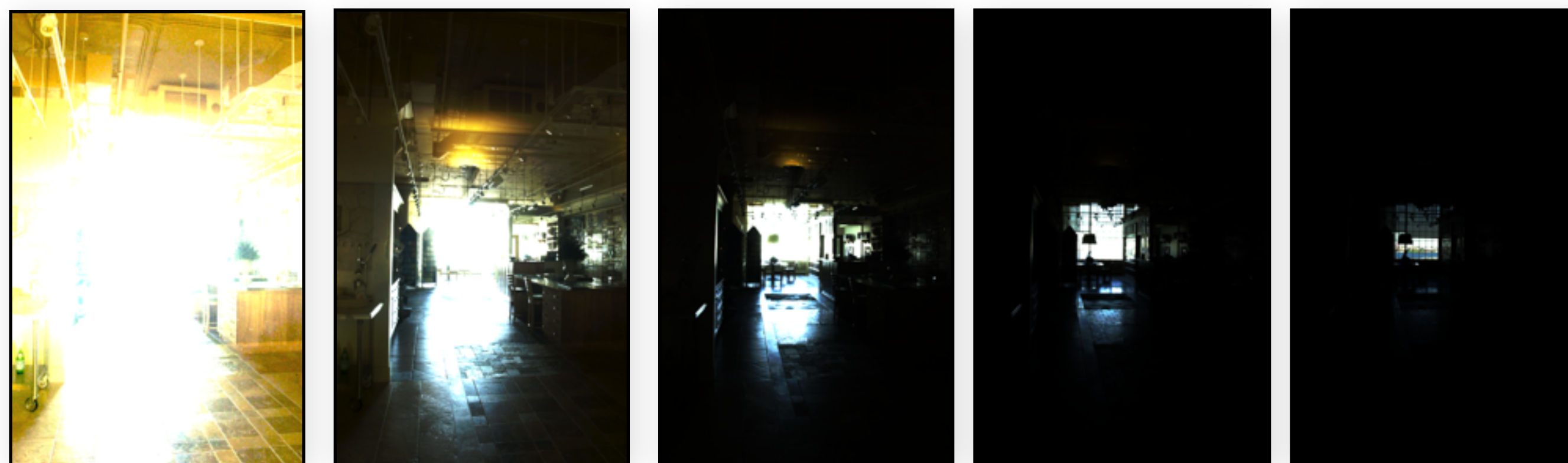
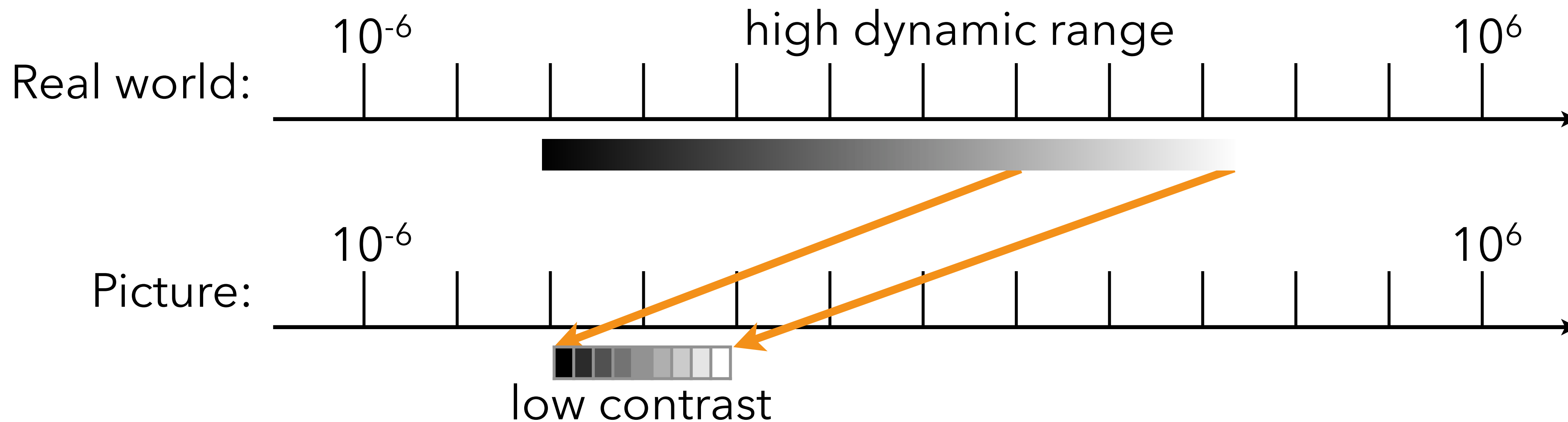
# Multiple exposure photography

Sequentially measure all segments of the range



# Multiple exposure photography

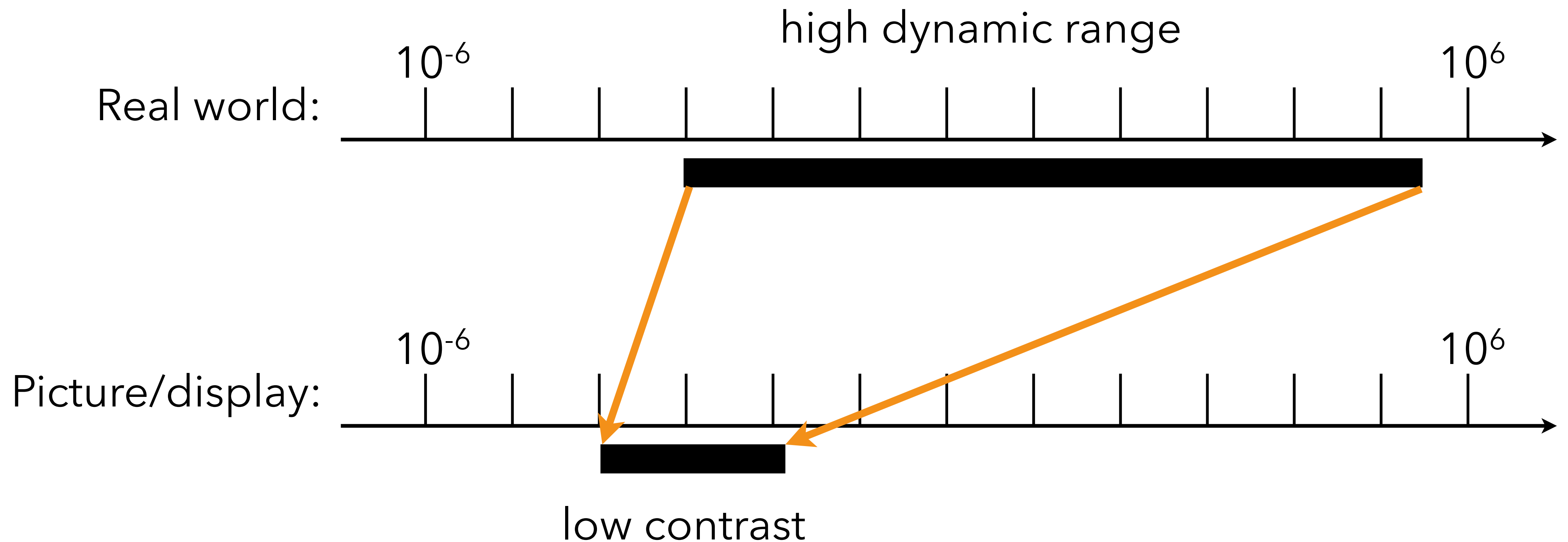
Sequentially measure all segments of the range





# Problem 2: Display the information

Match limited contrast of the medium while preserving details: the tone mapping problem





"Wielki Staw Polski"

[Wojciech Jarosz 2011]



"Wielki Staw Polski"

[Wojciech Jarosz 2011]

# Global tone mapping operators

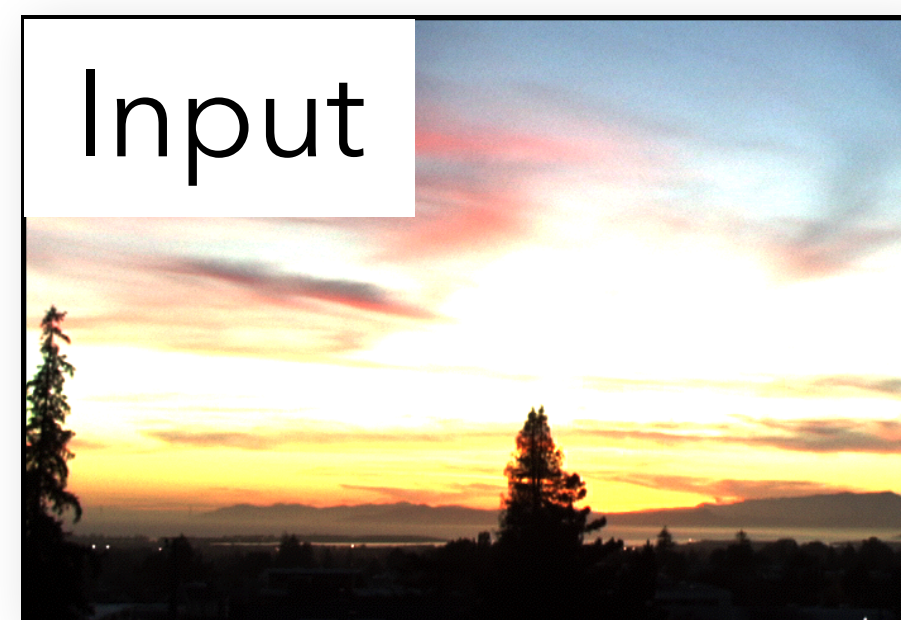
Gamma compression, applied independently on R,G,B

- output =  $e \cdot \text{input}^\gamma$  ( $\gamma = 0.5$  here)

Colors become washed-out.

- Why?

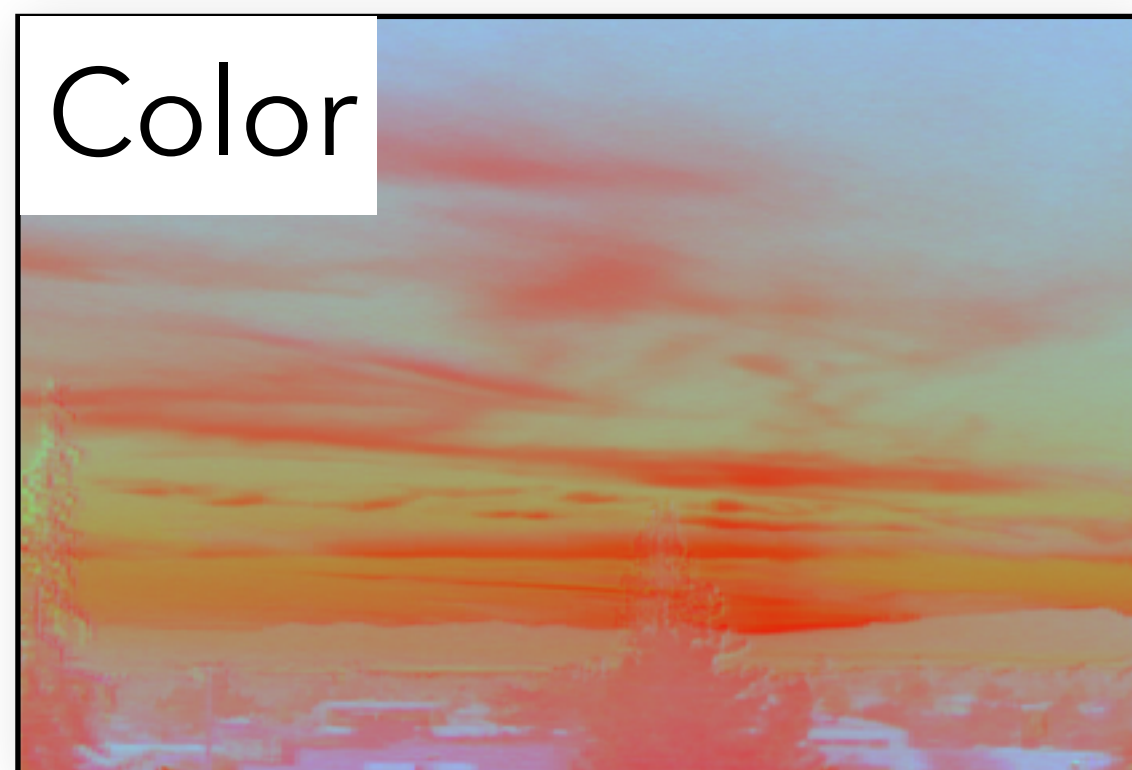
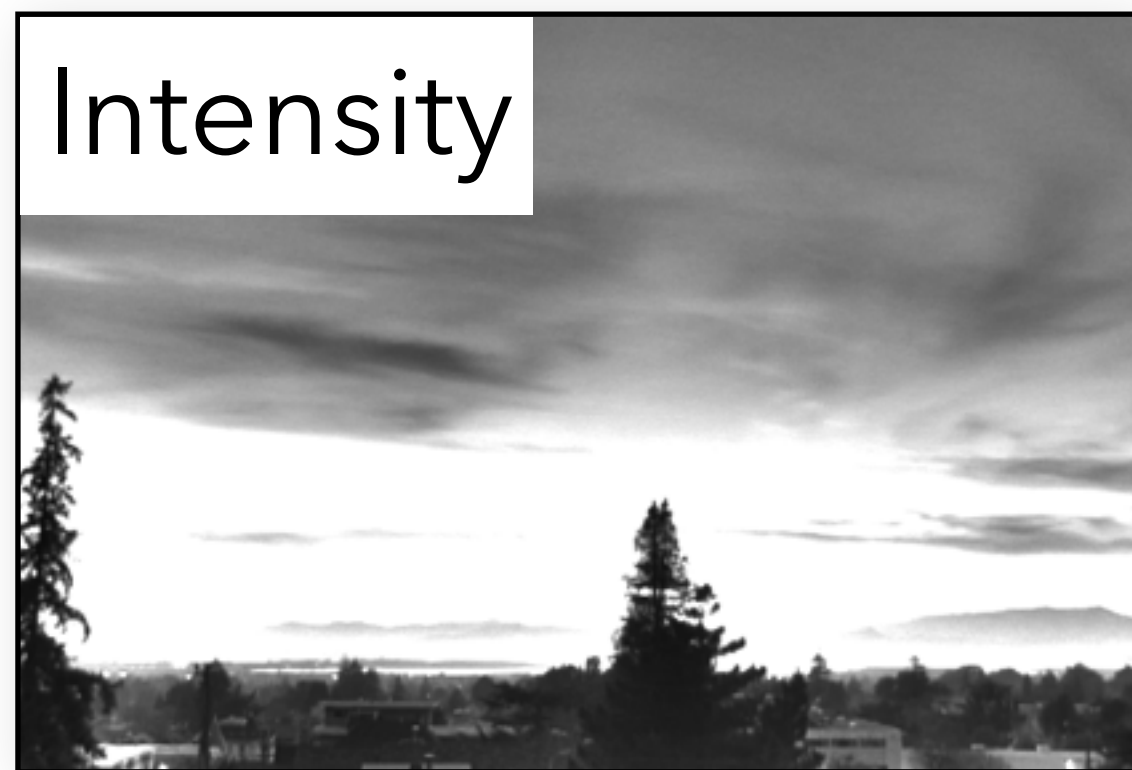
In addition to the gamma transform during RAW-to-JPEG conversion



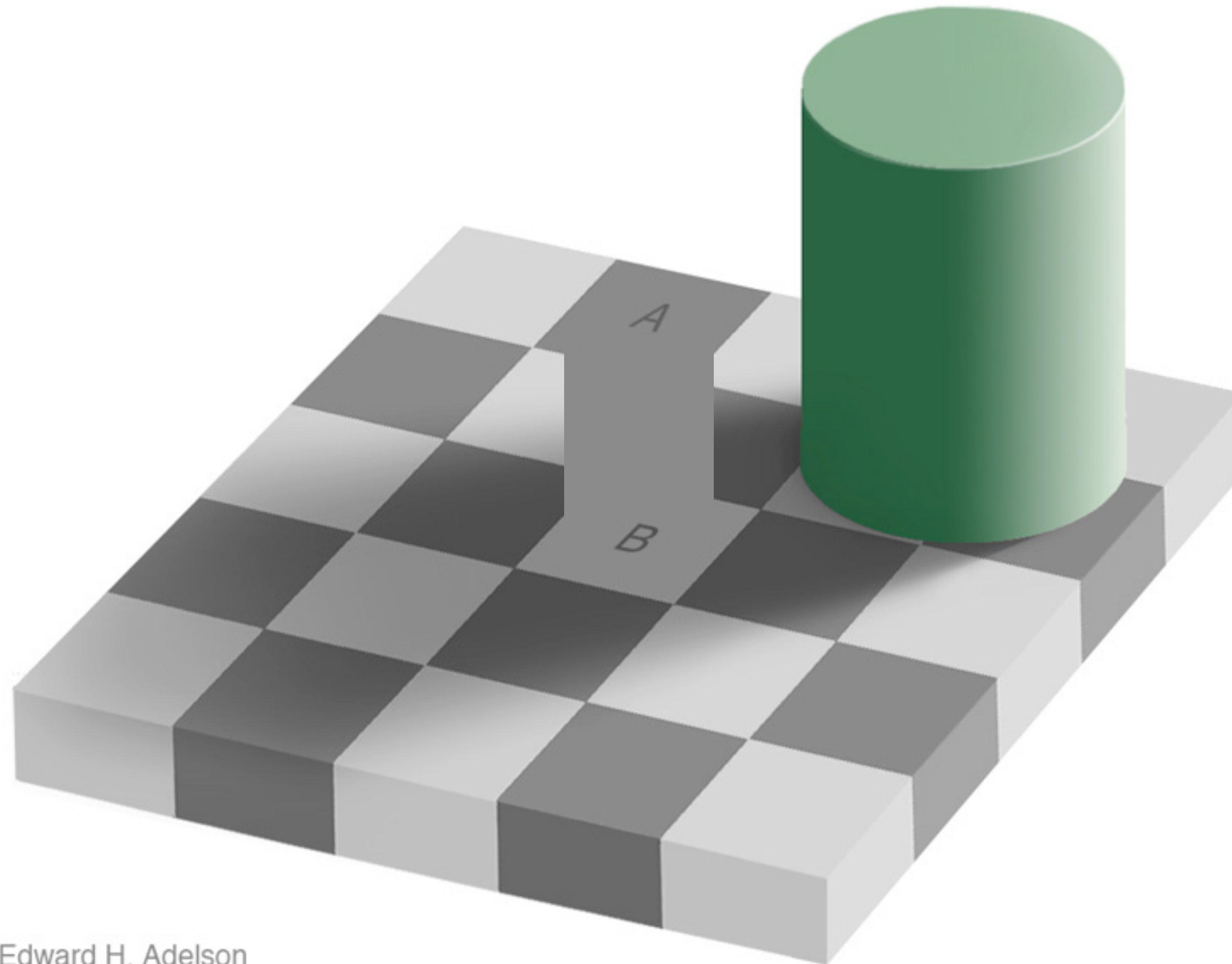
# Global tone mapping operators

Gamma compression on intensity only

Colors are OK, but details (high-frequency intensity) not



# The importance of local contrast



straight print



toned print



Ansel Adams, Clearing Winter Storm, 1942

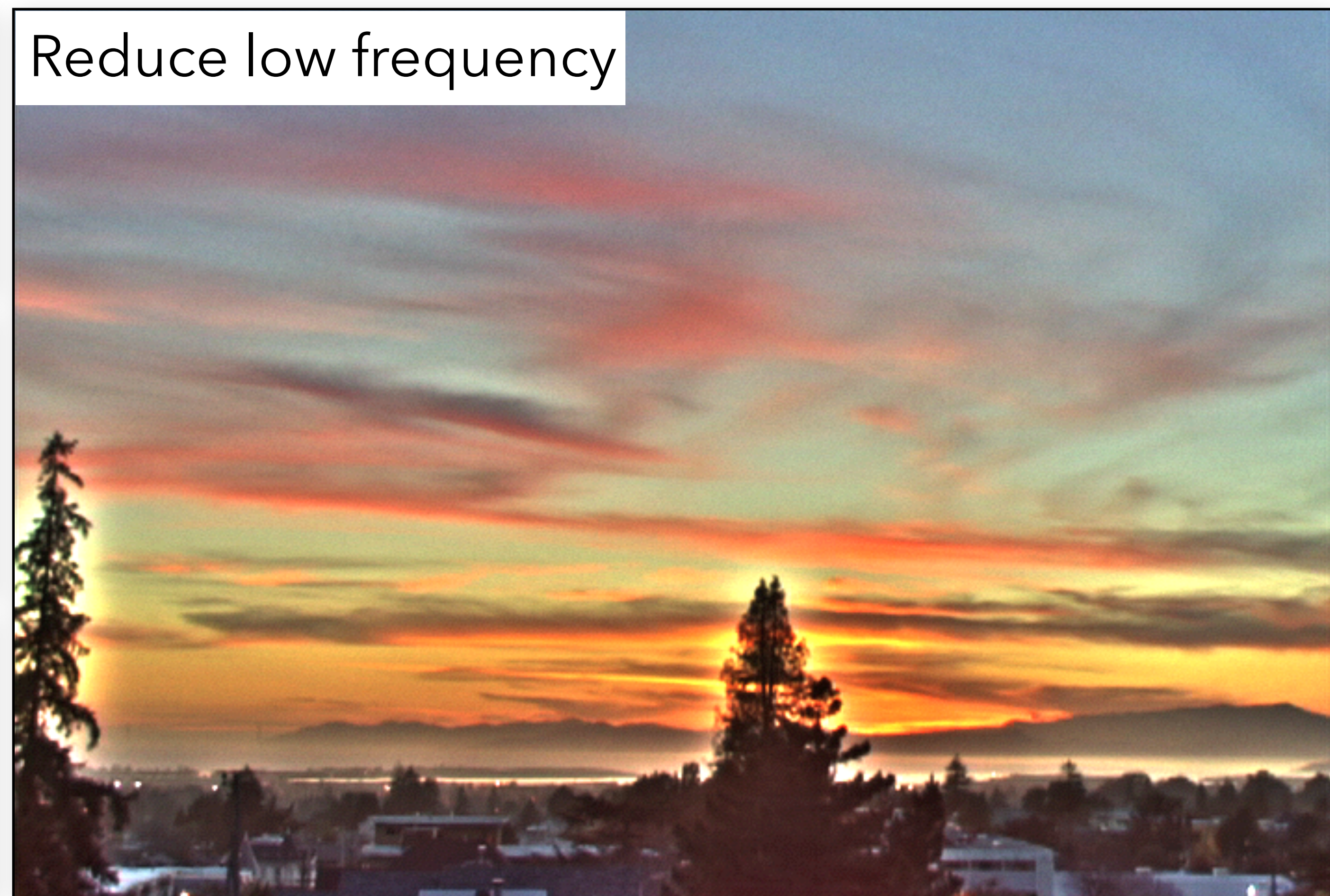
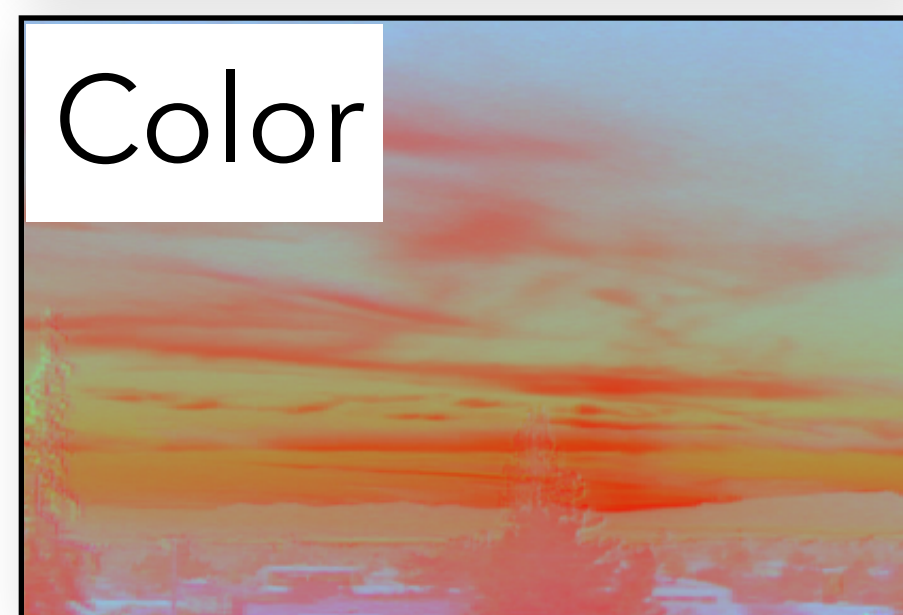
# La Grande Jatte, Georges Seurat, 1884





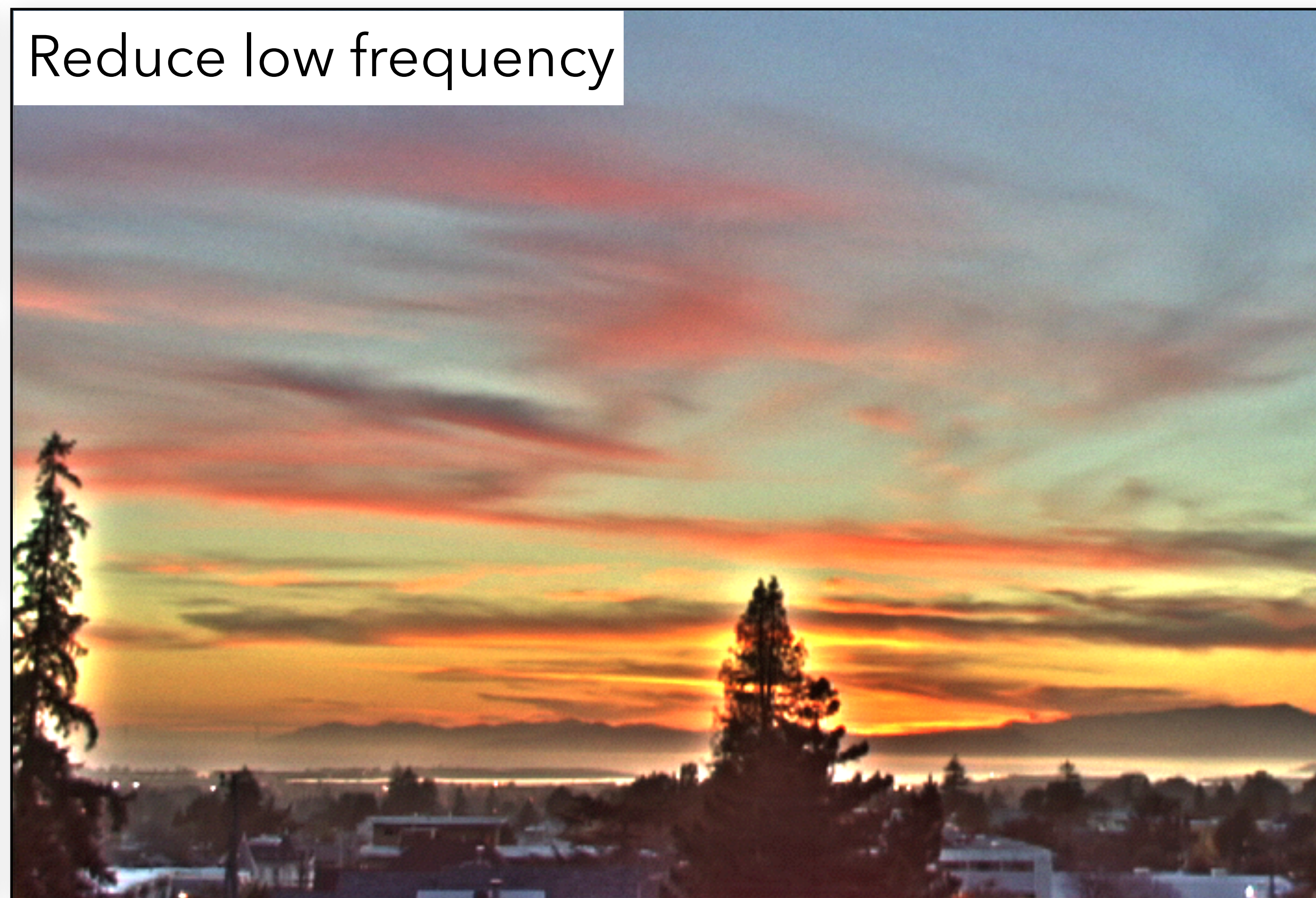
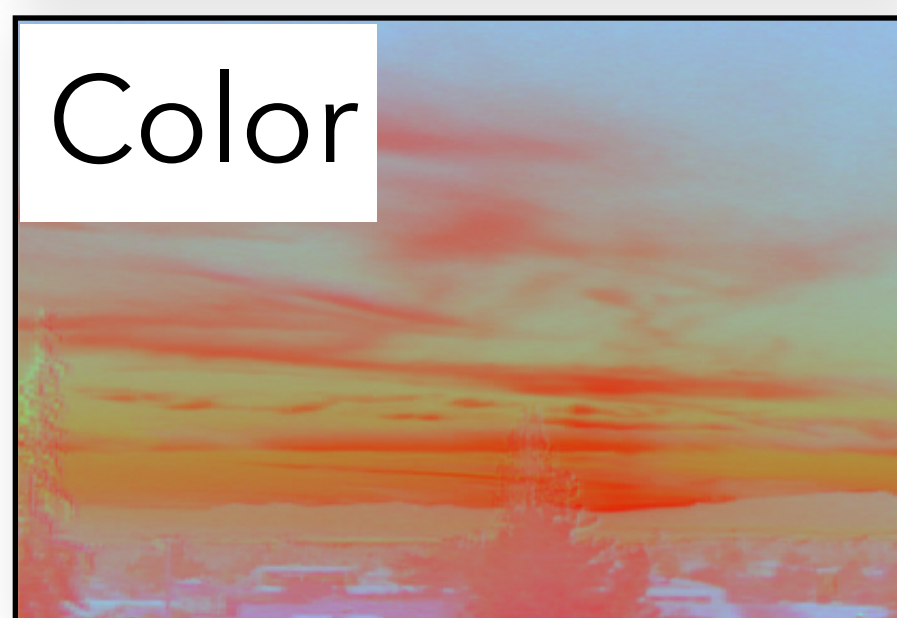
# Oppenheim 1968, Chiu et al. 1993

Reduce contrast of low-frequencies, preserve high frequencies

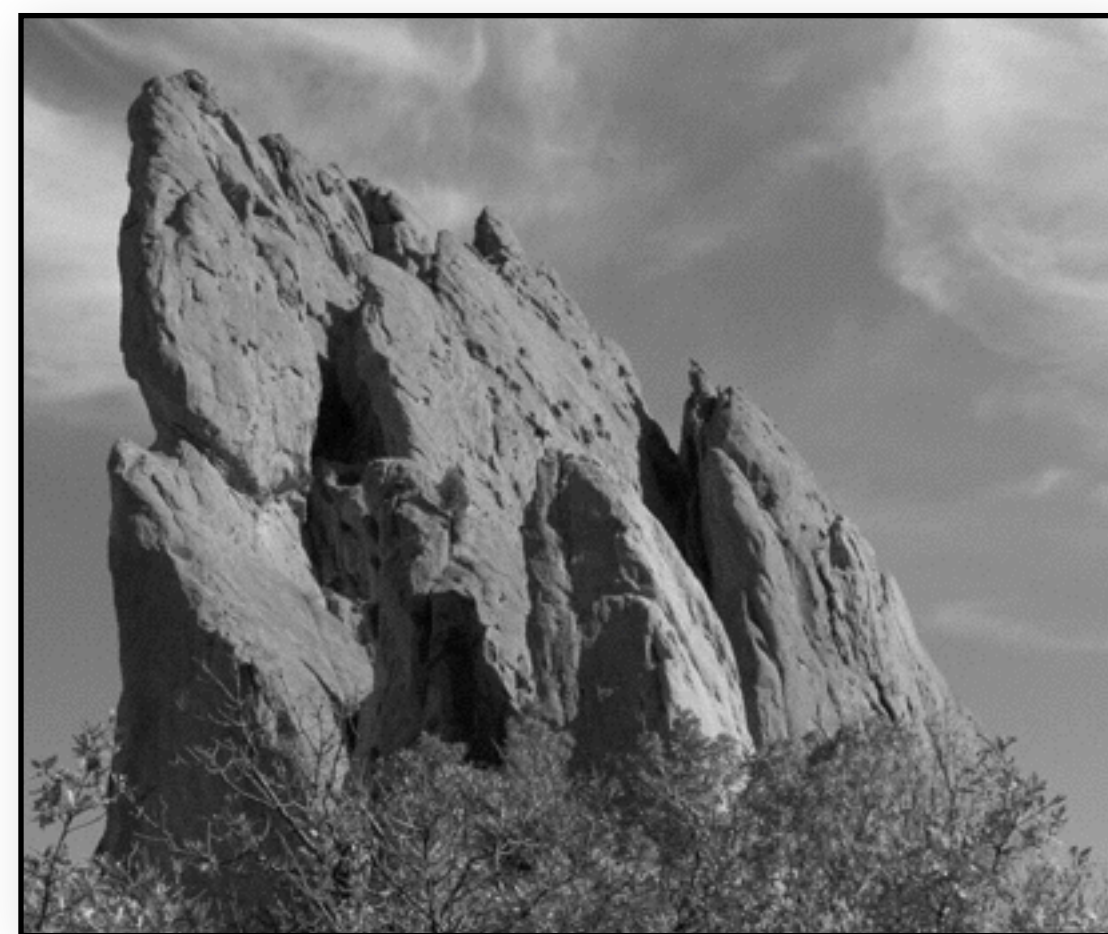


# The halo nightmare

For strong edges; because they contain high frequency



# Gaussian vs. Bilateral filter

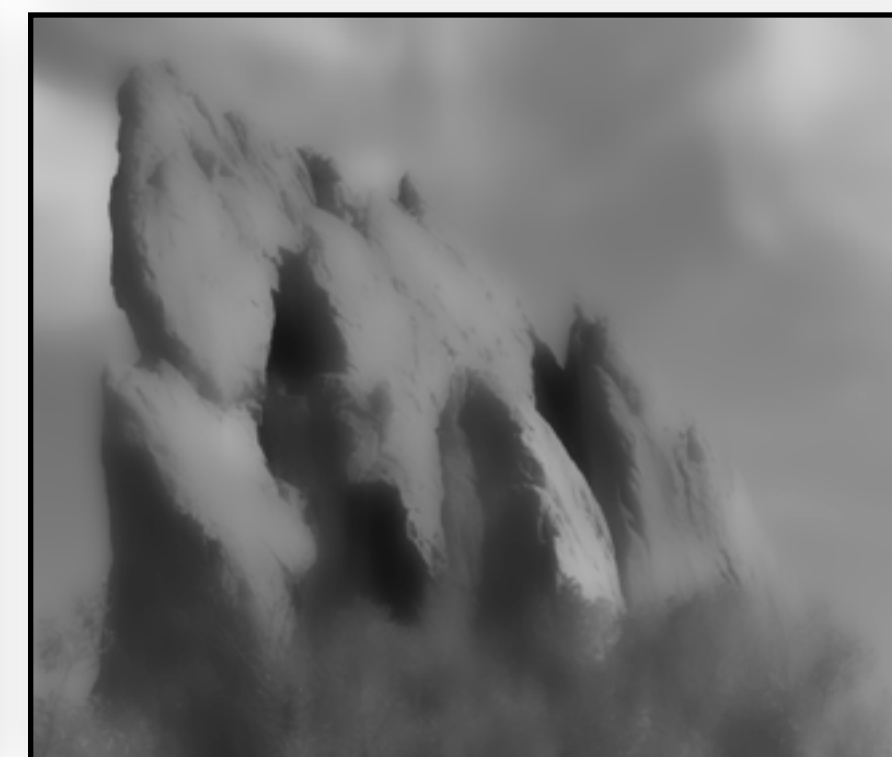


Input

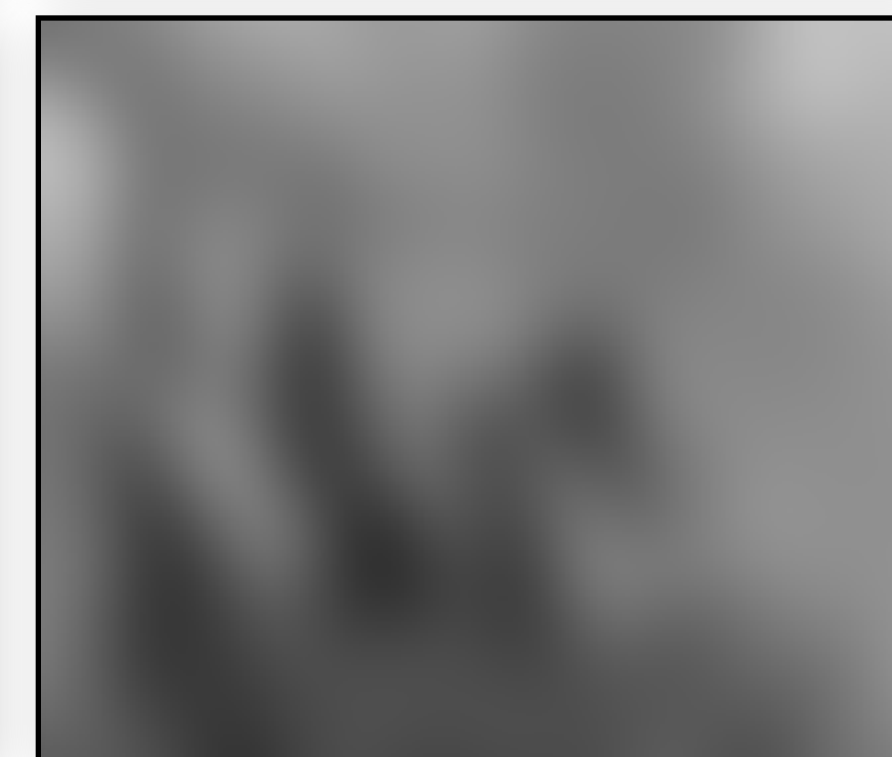
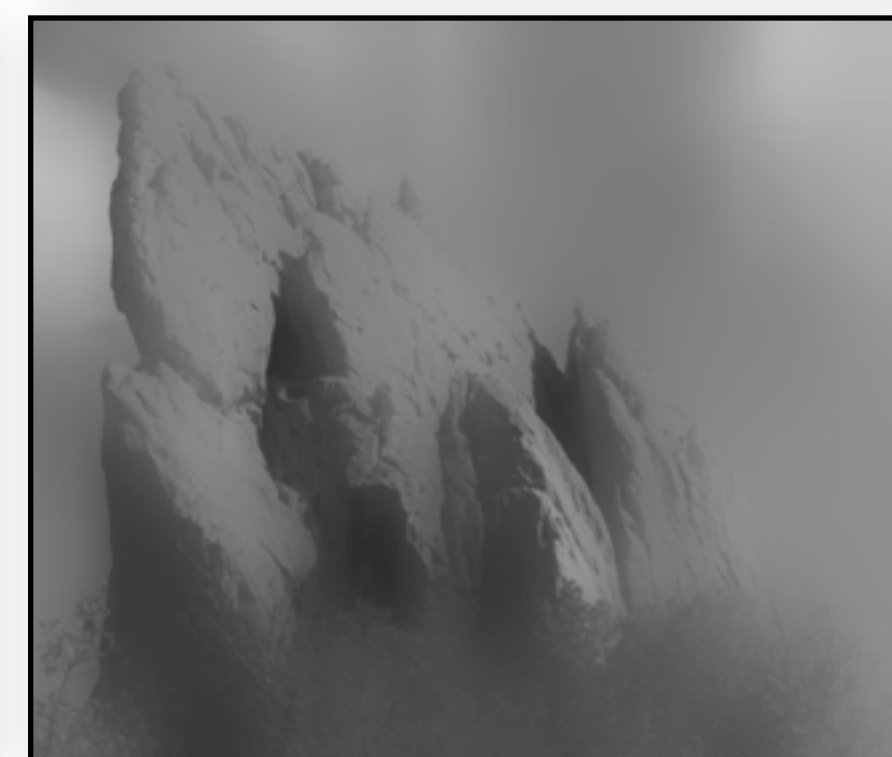
$$\sigma_s = 2$$



$$\sigma_s = 6$$



$$\sigma_s = 18$$



$$\sigma_r = 0.1$$

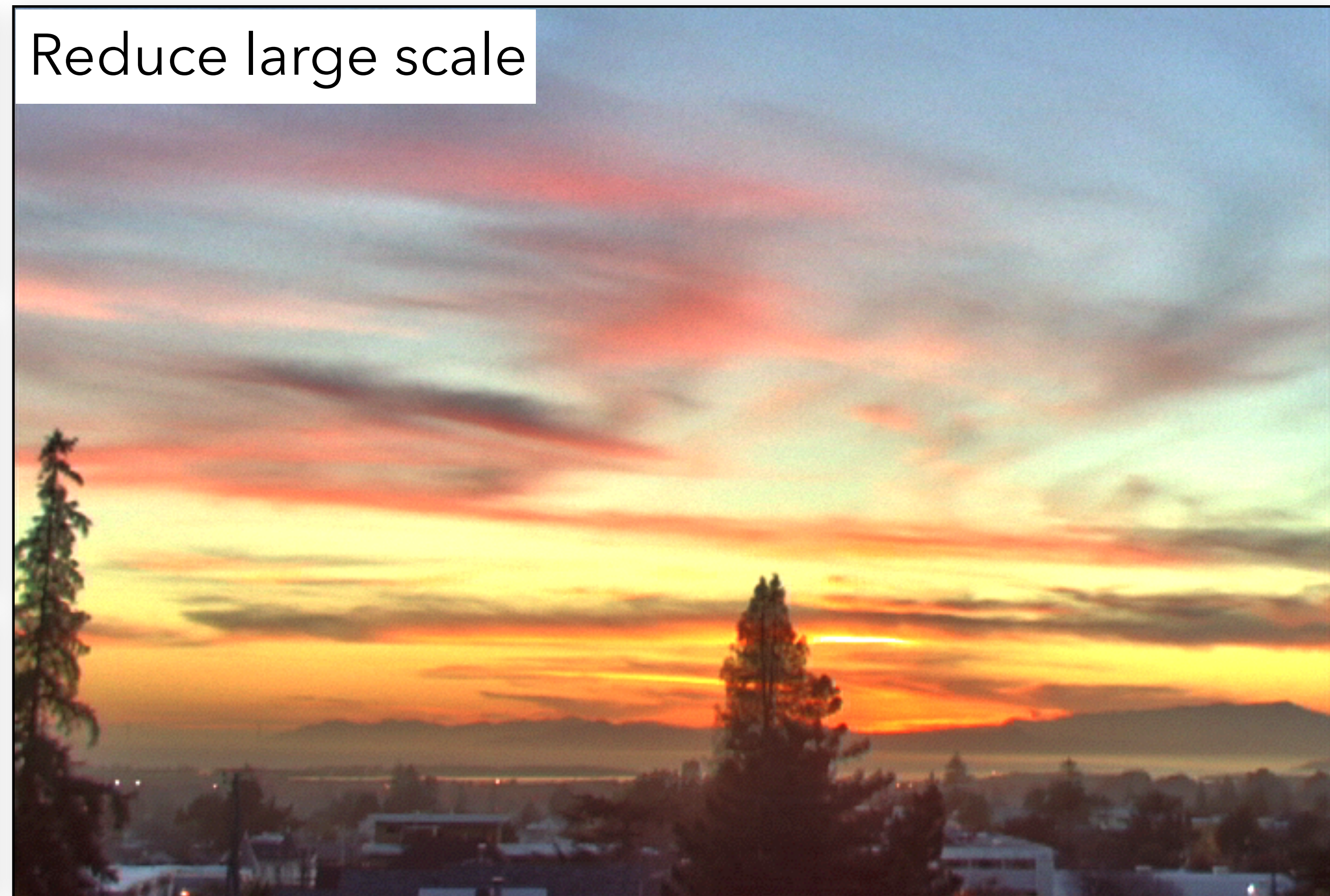
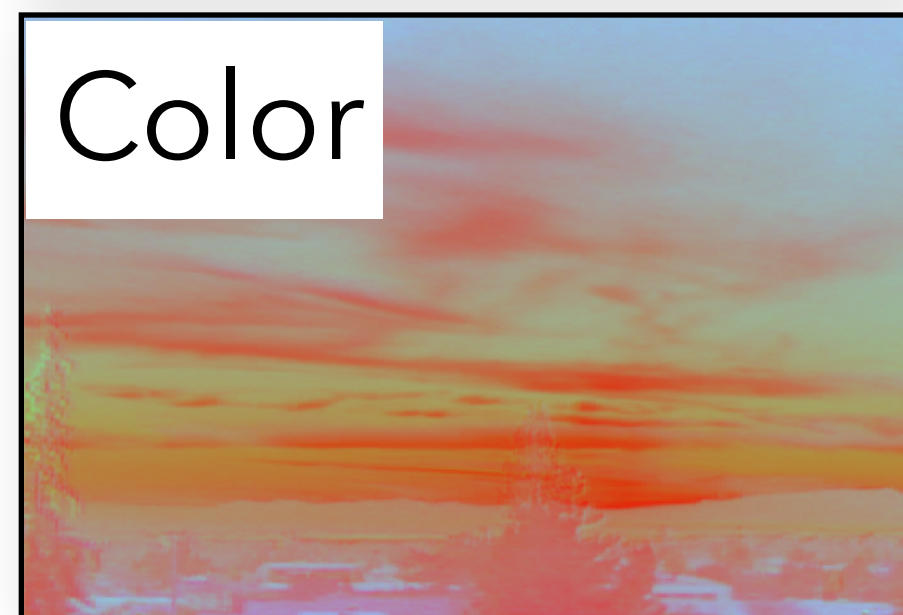
$$\sigma_r = 0.25$$

$$\sigma_r = \infty$$

(Gaussian blur)

# Durand and Dorsey 2002

Don't blur across edges, decompose using bilateral filter



# Today

---

Recap of bilateral tone mapping

Variance-optimized weights for HDR merging

HDR merging/tone mapping in practice

# Contrast reduction

Input HDR image



Contrast  
too high!

# Contrast reduction

Input HDR image



Intensity



$$\text{intensity} = 0.4R + 0.7G + 0.01B$$

Color



$$\begin{aligned} R' &= R / \text{intensity} \\ G' &= G / \text{intensity} \\ B' &= B / \text{intensity} \end{aligned}$$

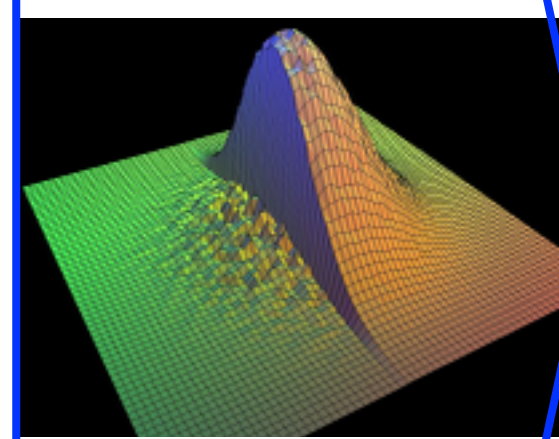
important to use ratios  
(makes it luminance  
invariant)

# Contrast reduction

Input HDR image



Intensity



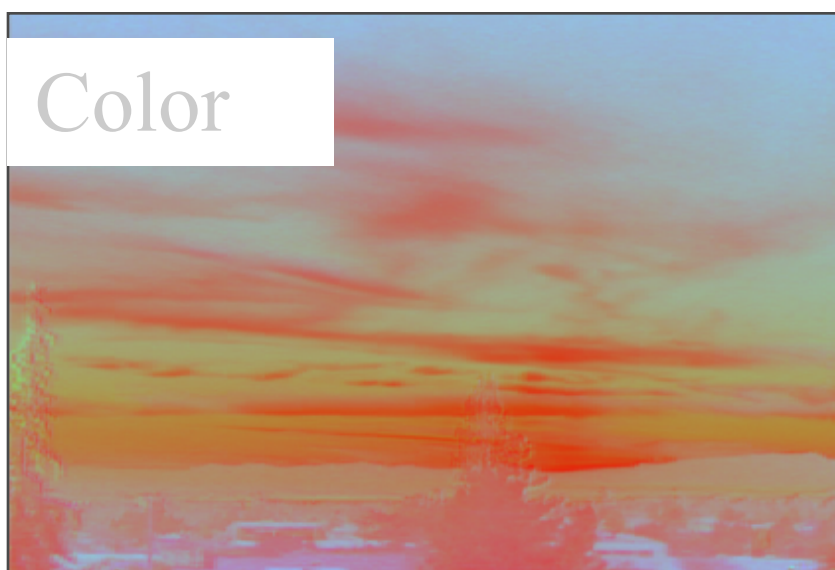
Large scale



Bilateral  
Filter

in log

Color



Spatial sigma: 2 to 5% image size  
Range sigma: 0.4 (in log 10)

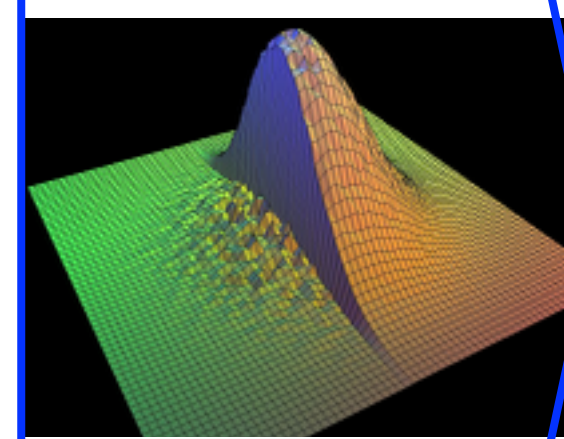


# Contrast reduction

Input HDR image



Intensity



Bilateral  
Filter  
in log

Large scale

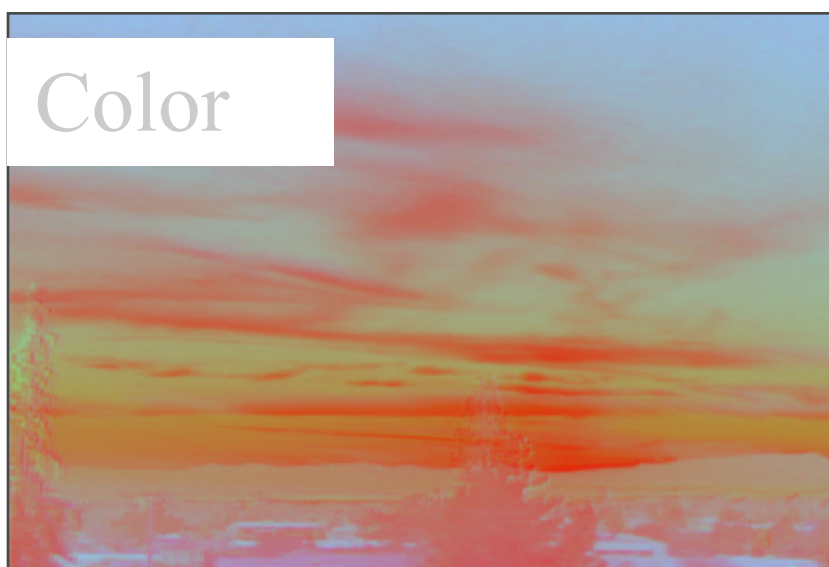


Detail



Detail = log intensity - large scale  
(residual)

Color

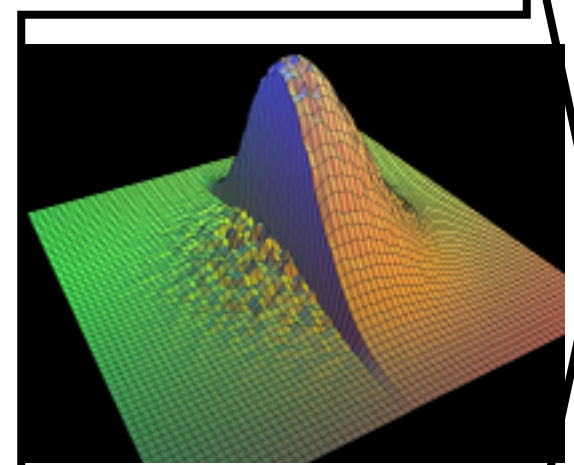


# Contrast reduction

Input HDR image



Intensity



Bilateral  
Filter  
in log

Large scale

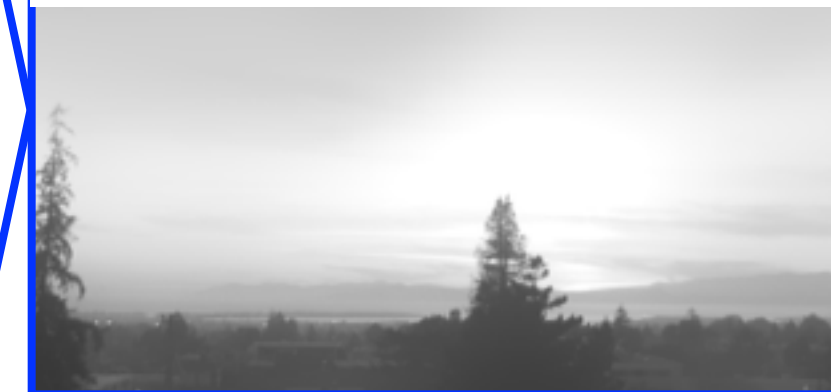


Detail

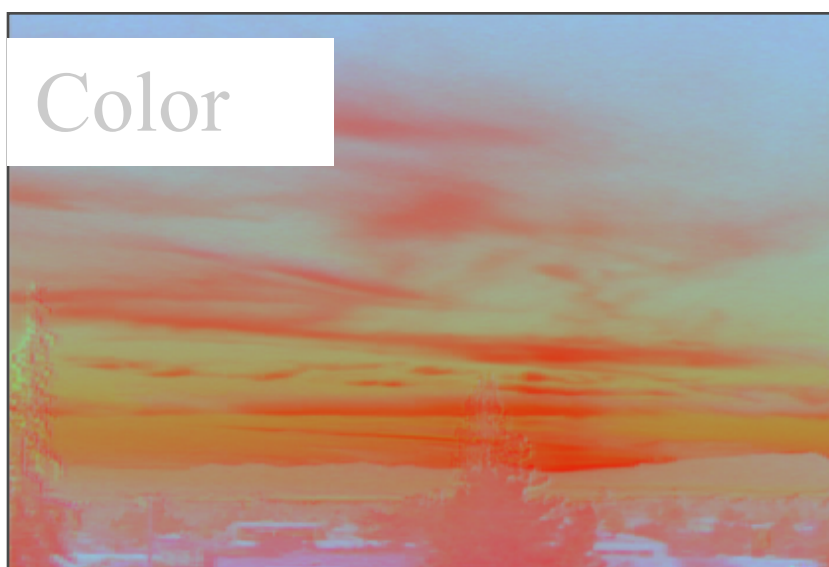


Reduce  
contrast

Large scale



Color

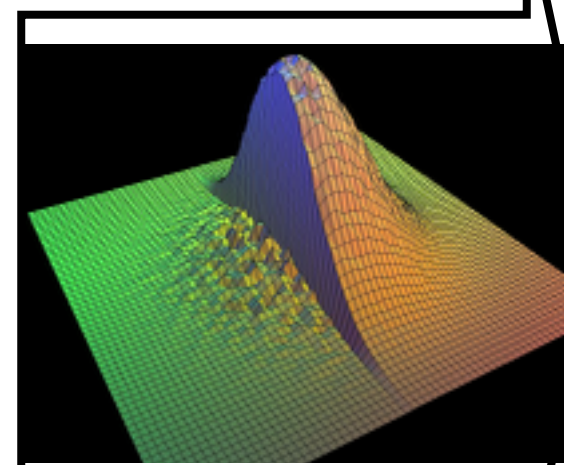


# Contrast reduction

Input HDR image



Intensity



Bilateral  
Filter  
in log

Large scale



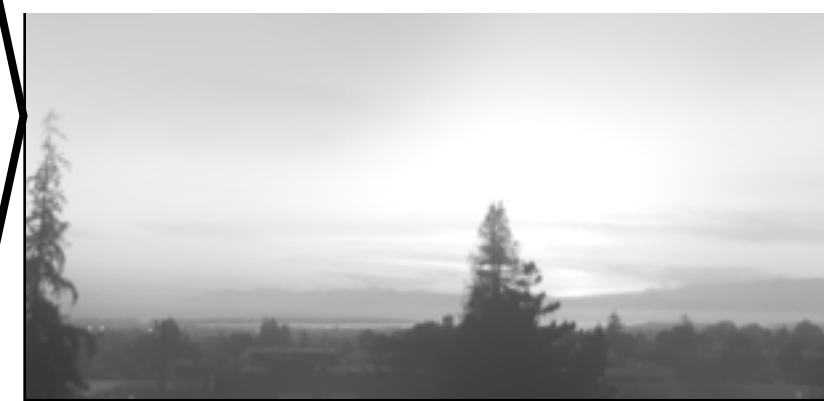
Detail



Reduce  
contrast

Preserve!

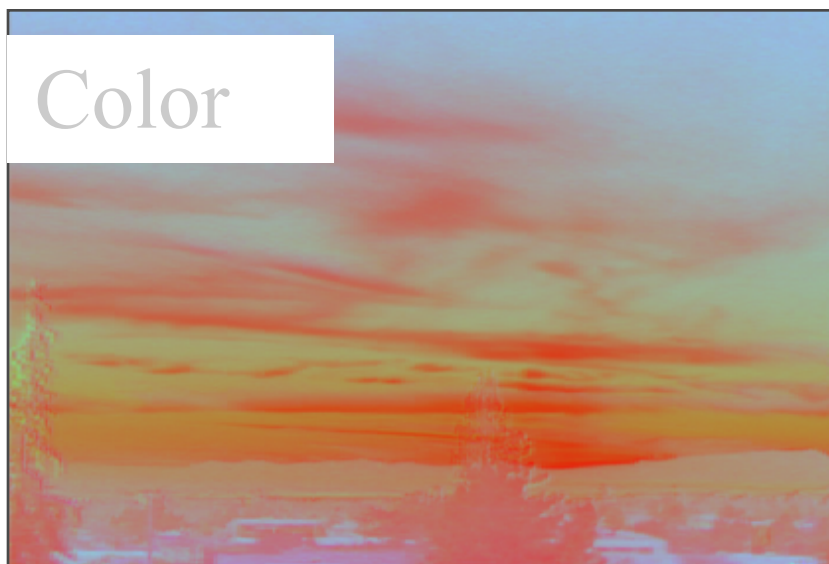
Large scale



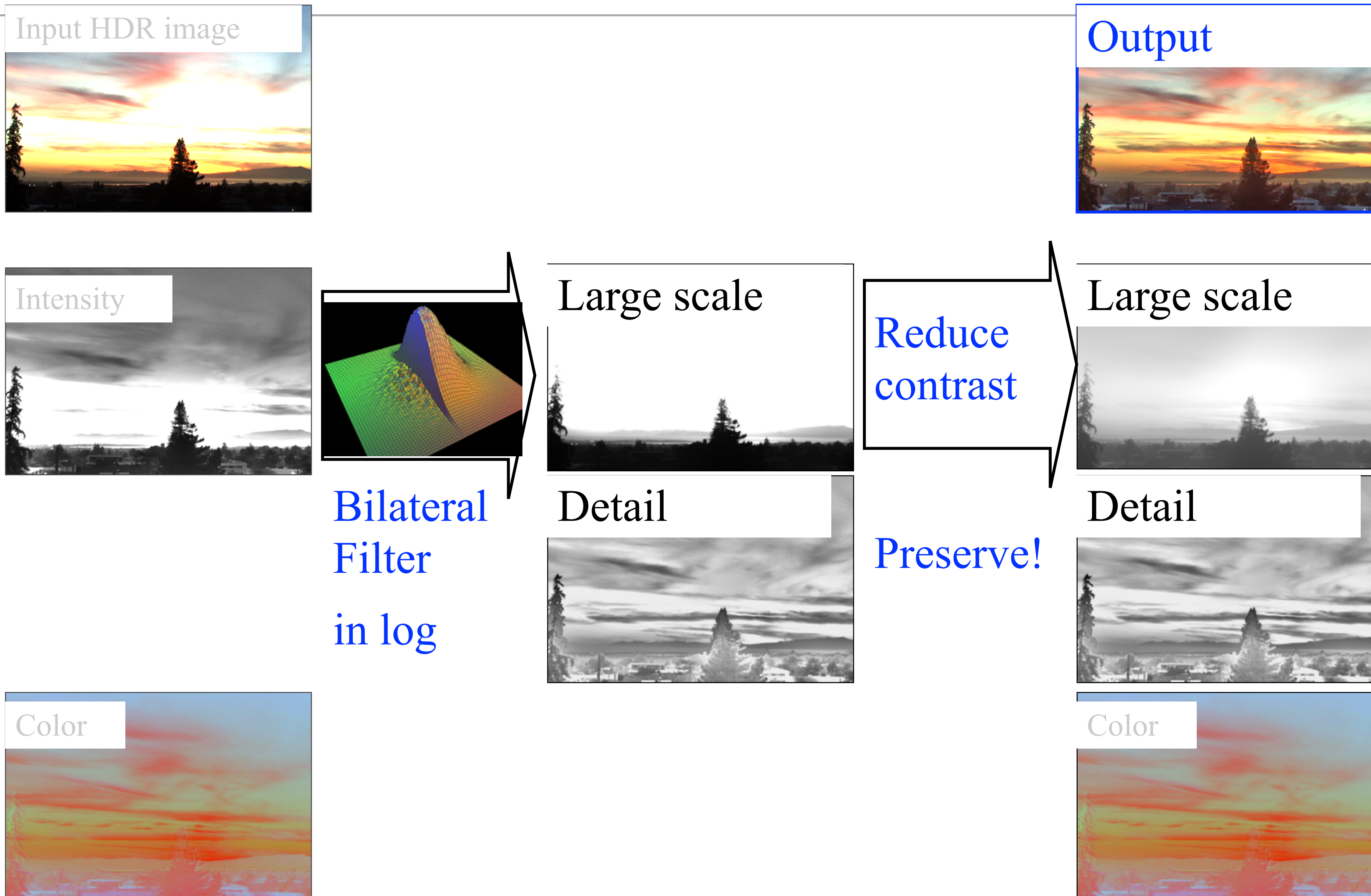
Detail



Color



# Contrast reduction



# Log domain

---

Very important to work in the log domain

Recall: humans are sensitive to multiplicative contrast

With log domain, our notion of “strong edge”  
always corresponds to the same contrast

# Scale decomposition in log domain

$$\text{inLog} = \log_{10}(\text{intensity})$$

$$\text{inLogLarge} = \text{bilateralFilter}(\text{inLog})$$

$$\text{inLogDetail} = \text{inLog} - \text{inLogLarge}$$

hence:

- $\text{inLog} = \text{inLogDetail} + \text{inLogLarge}$ , or
- $\text{intensity} = 10^{\text{inLogDetail}} * 10^{\text{inLogLarge}}$

Now manipulate large-scale and detail separately

# Contrast reduction **in log domain**

$$\text{outLog} = \text{inLogDetail} + k * (\text{inLogLarge} - \max(\text{inLogLarge}))$$

Normalize so that the biggest value is 0 in log

Set target large-scale contrast (e.g.  $\text{targetRange} = \log_{10}(100)$ )

- i.e. in **linear** output, we want 1:100 contrast for large scale

Compute range of input's large-scale layer:

-  $\text{largeRange} = \max(\text{inLogLarge}) - \min(\text{inLogLarge})$

Scale factor  $k = \text{targetRange} / \text{largeRange}$

# Contrast reduction **in log domain**

$$\text{outLog} = \text{detailAmp} * \text{inLogDetail} + k * (\text{inLogLarge} - \max(\text{inLogLarge}))$$

Normalize so that the biggest value is 0 in log

Set target large-scale contrast (e.g.  $\text{targetRange} = \log_{10}(100)$ )

- i.e. in **linear** output, we want 1:100 contrast for large scale

Compute range of input's large-scale layer:

-  $\text{largeRange} = \max(\text{inLogLarge}) - \min(\text{inLogLarge})$

Scale factor  $k = \text{targetRange} / \text{largeRange}$

**Optional:** amplify detail by detailAmp



# Final output

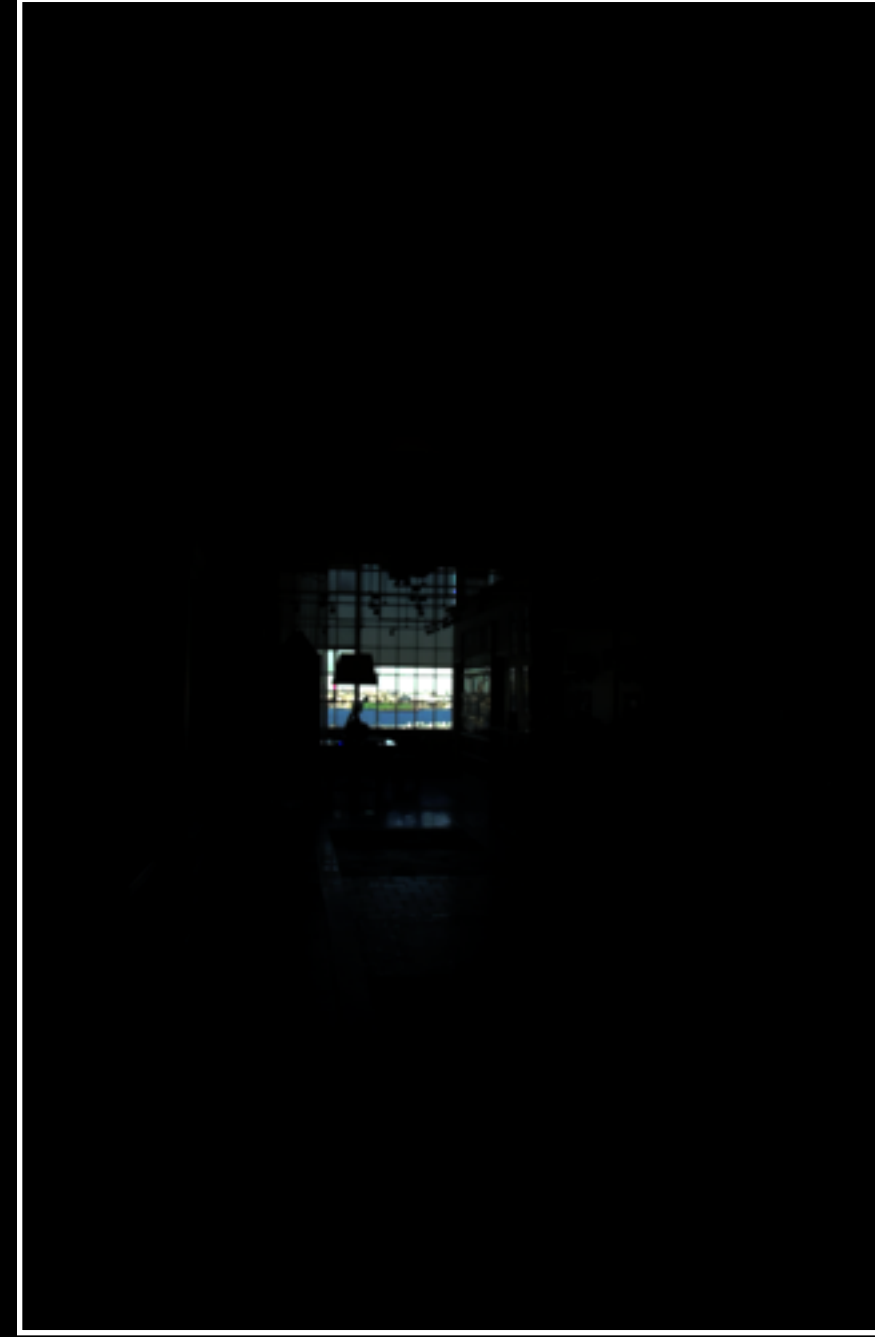
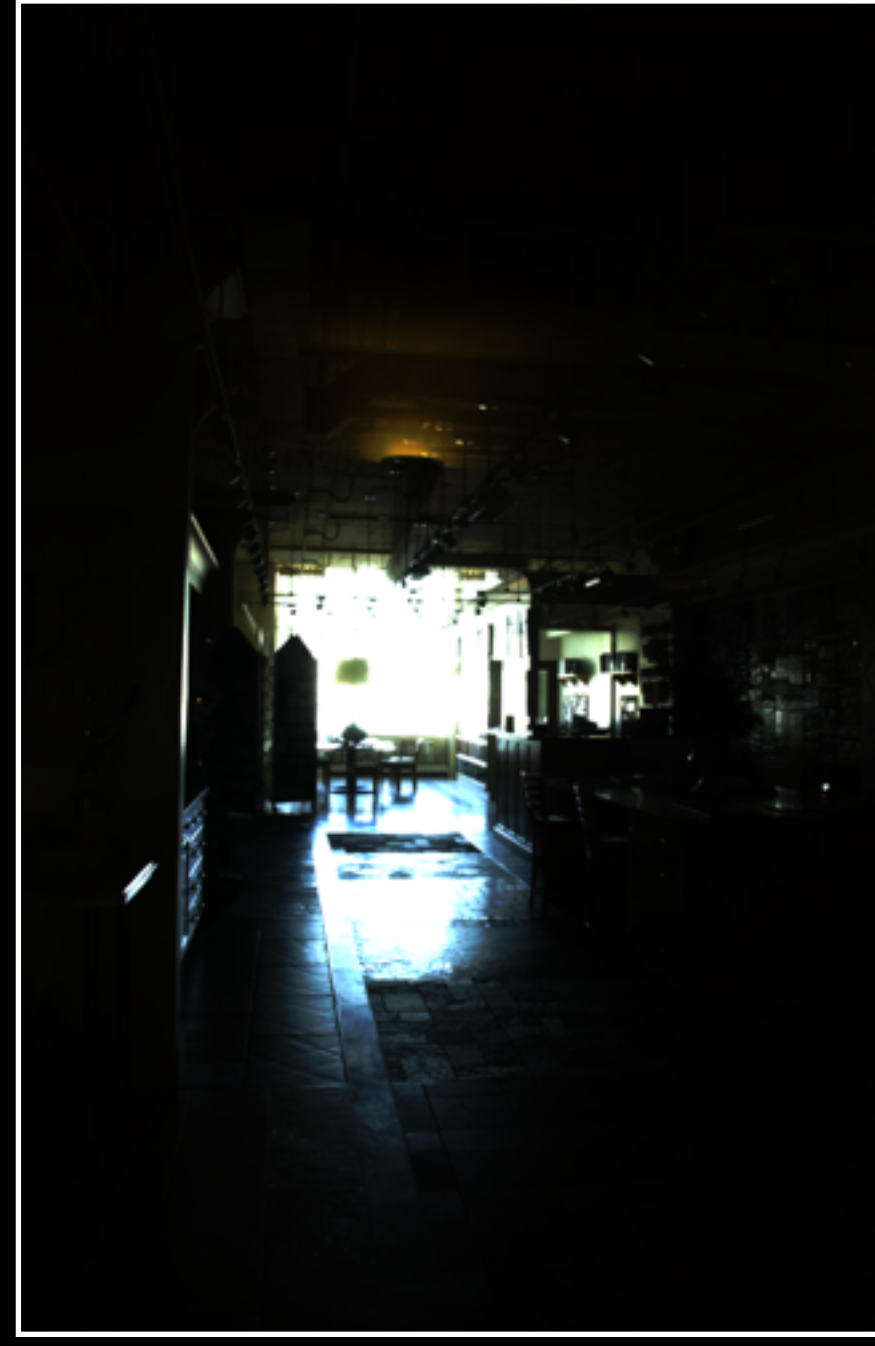
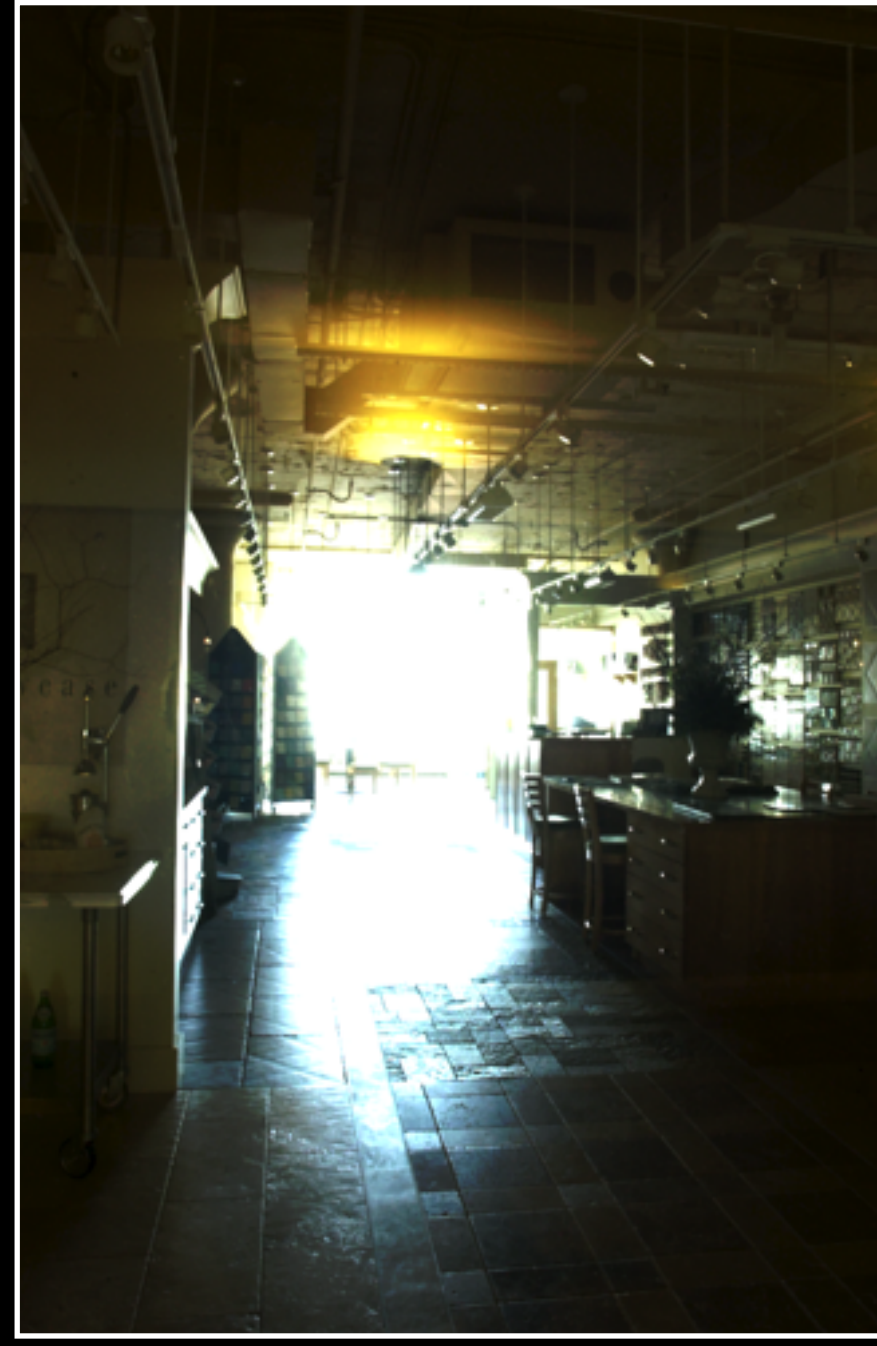
$$\text{outLog} = \text{detailAmp} * \text{inLogDetail} + k * (\text{inLogLarge} - \max(\text{inLogLarge}))$$

$$\text{outIntensity} = 10^{\text{outLog}}$$

Recall that  $R', G', B'$  is the intensity-normalized RGB color

- $\text{outR} = \text{outIntensity} * R'$
- $\text{outG} = \text{outIntensity} * G'$
- $\text{outB} = \text{outIntensity} * B'$

After a slide by Frédo Durand



# What matters

---

Spatial sigma: not very important

Range sigma: quite important

Use of the log domain for range: **critical**

- Because HDR and because perception sensitive to multiplicative contrast

# Speed

---

Direct bilateral filtering is slow (minutes)

Fast algorithm: bilateral grid

- <http://groups.csail.mit.edu/graphics/bilagrid/>
- [http://people.csail.mit.edu/sparis/publi/2009/ijcv/Paris\\_09\\_Fast\\_Approximation.pdf](http://people.csail.mit.edu/sparis/publi/2009/ijcv/Paris_09_Fast_Approximation.pdf)
- <http://graphics.stanford.edu/papers/gkdtrees/>

# Questions?

---

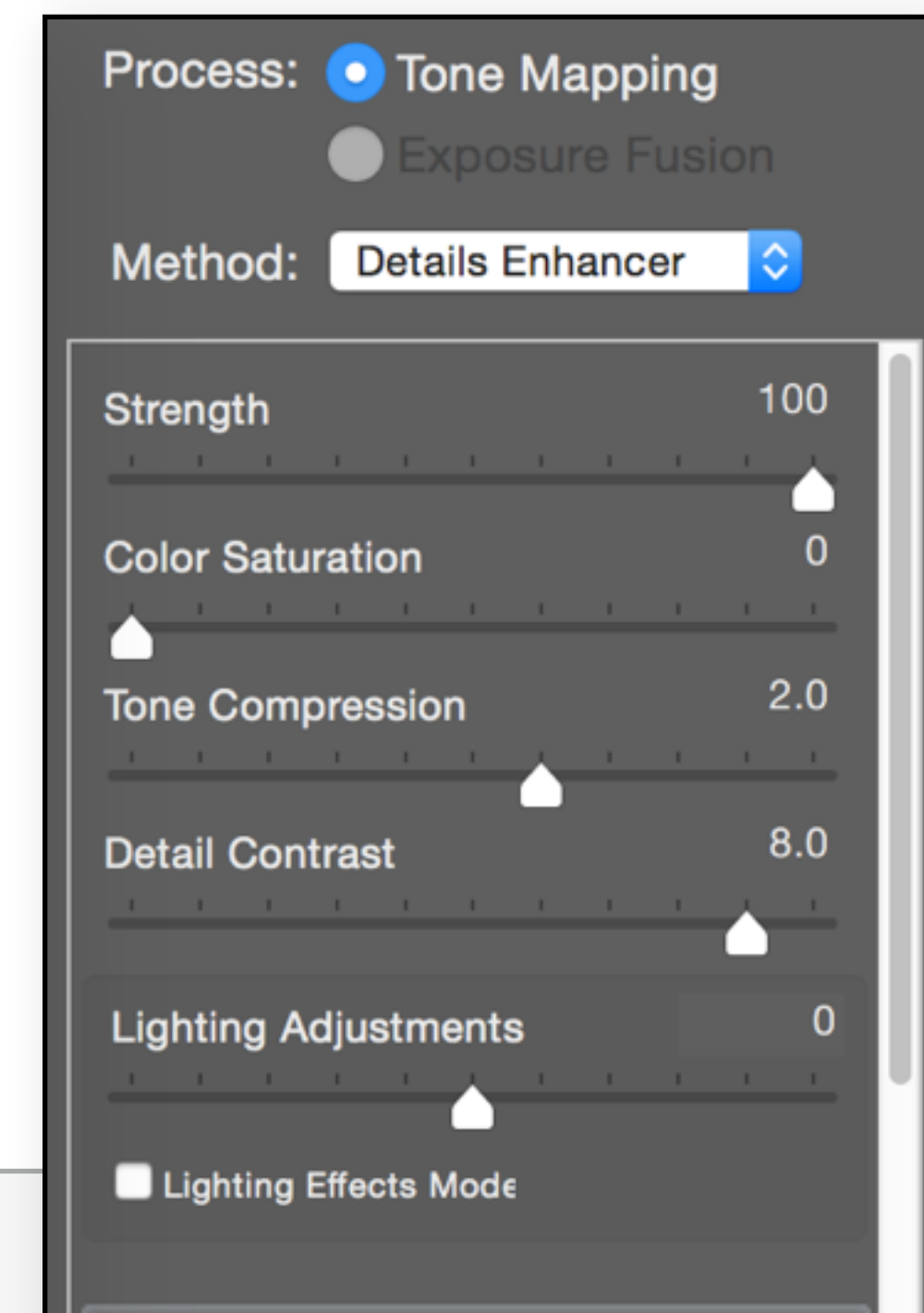
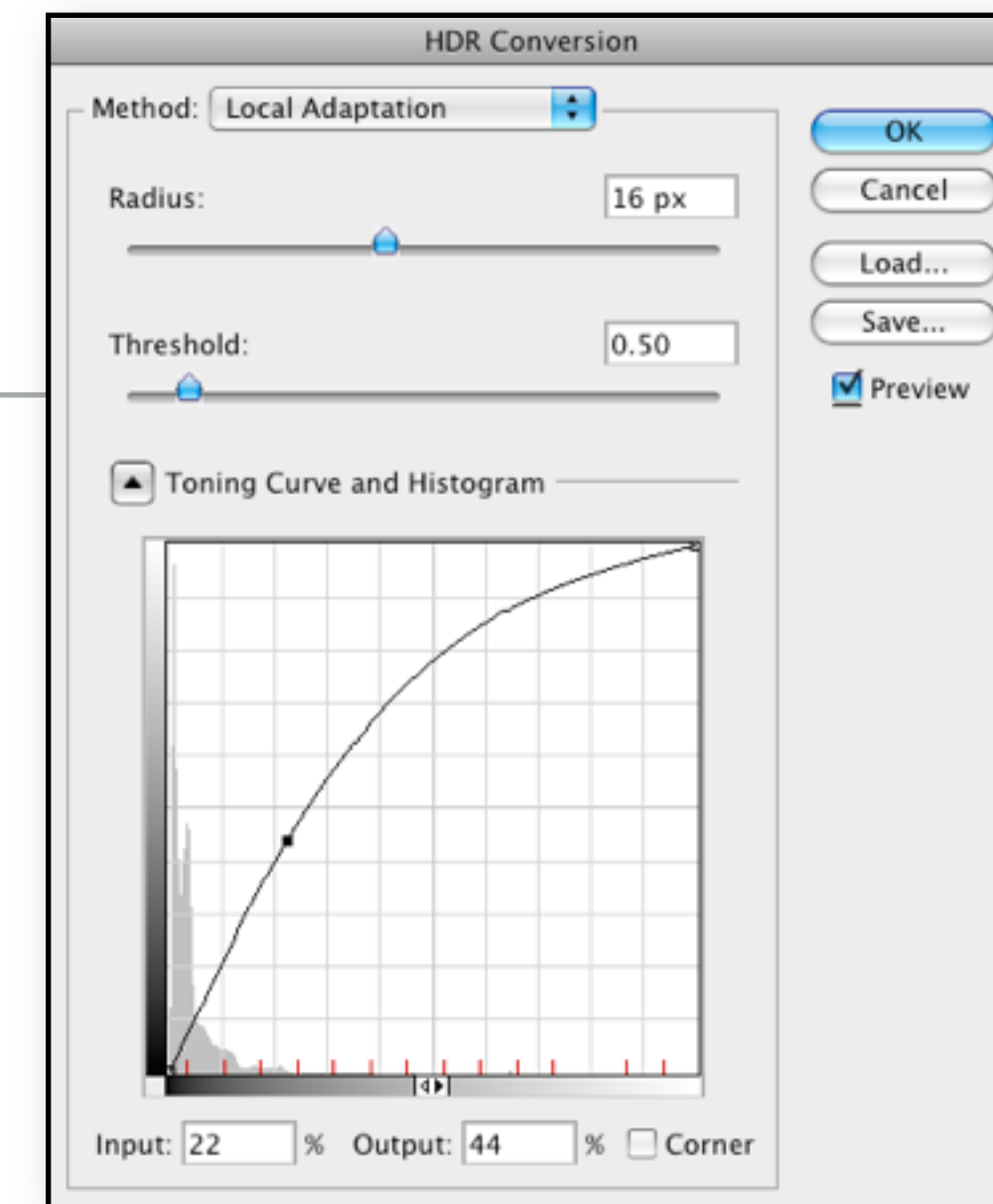
# Related tools

Photoshop "Local adaptation"

Lightroom "Fill Light"

- or "Shadows" (but with Local Laplacian Filter)

Photomatix "Details Enhancer"



# HDR vs. Tone mapping vs. Developing

---

Tone mapping is not something new or unique to HDR

- dodge-burn, dark room development, RAW processing

Your camera does tone mapping even if you don't do HDR

Film & digital SLRs have more dynamic range than display

- Enhance/preserve details, map larger range to smaller

HDR tone mapping and RAW processing (e.g. Lightroom Develop module) are doing fundamentally similar things



"Abandoned Ship at Point Reyes"

[Wojciech Jarosz 2014]





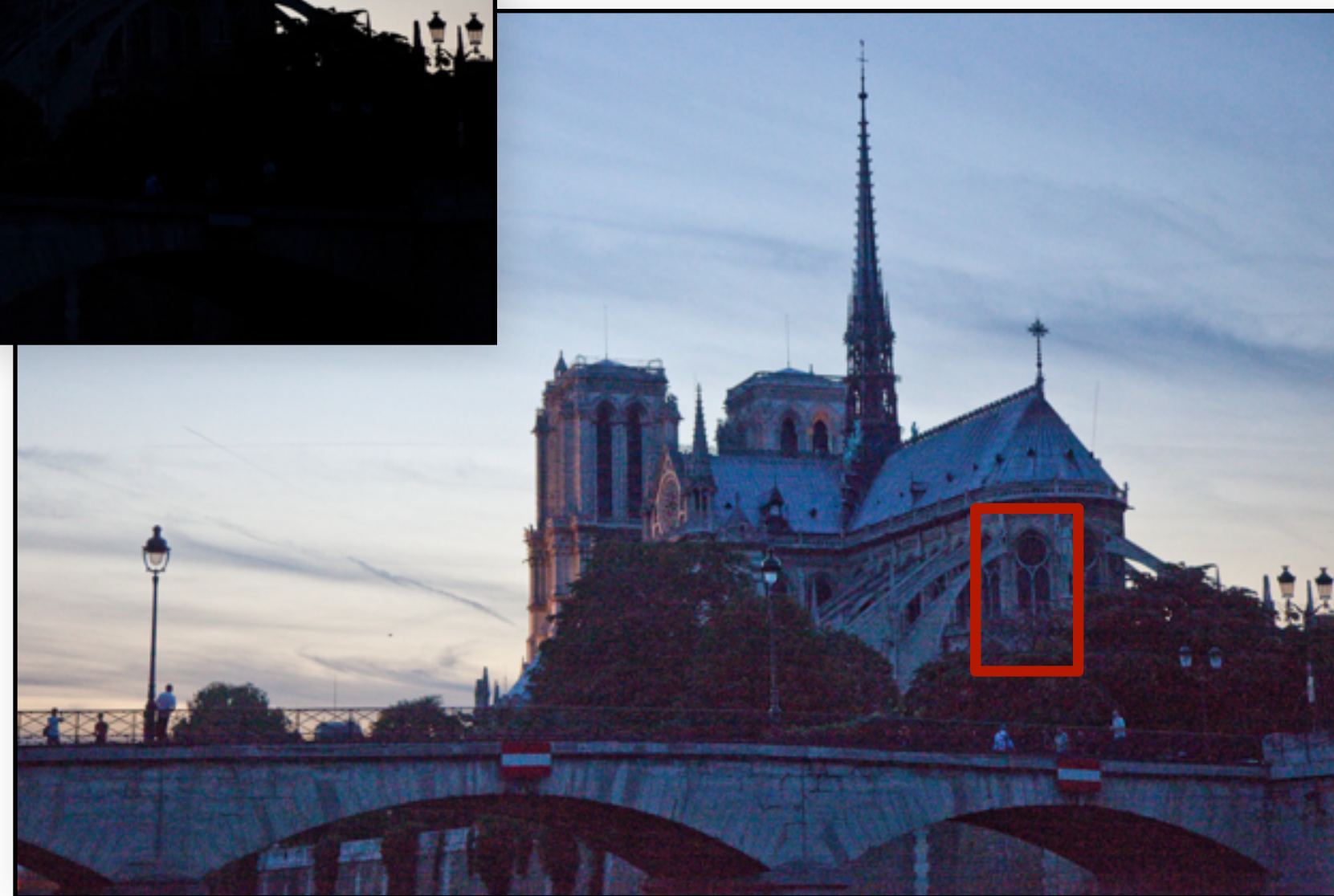
POINT REYES

"Abandoned Ship at Point Reyes"

[Wojciech Jarosz 2014]

# Up to a point

Noise gets amplified in the shadows

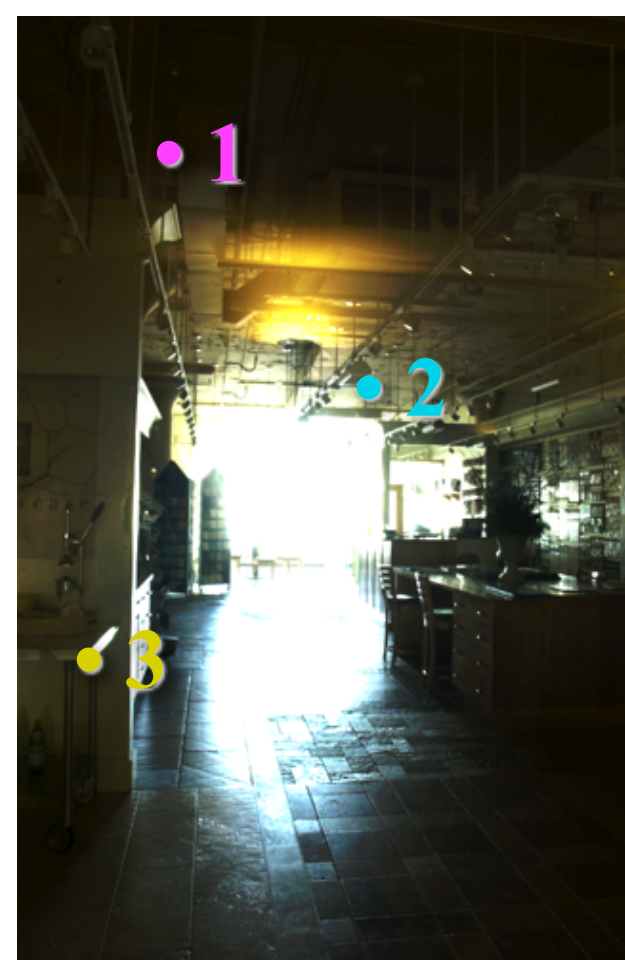
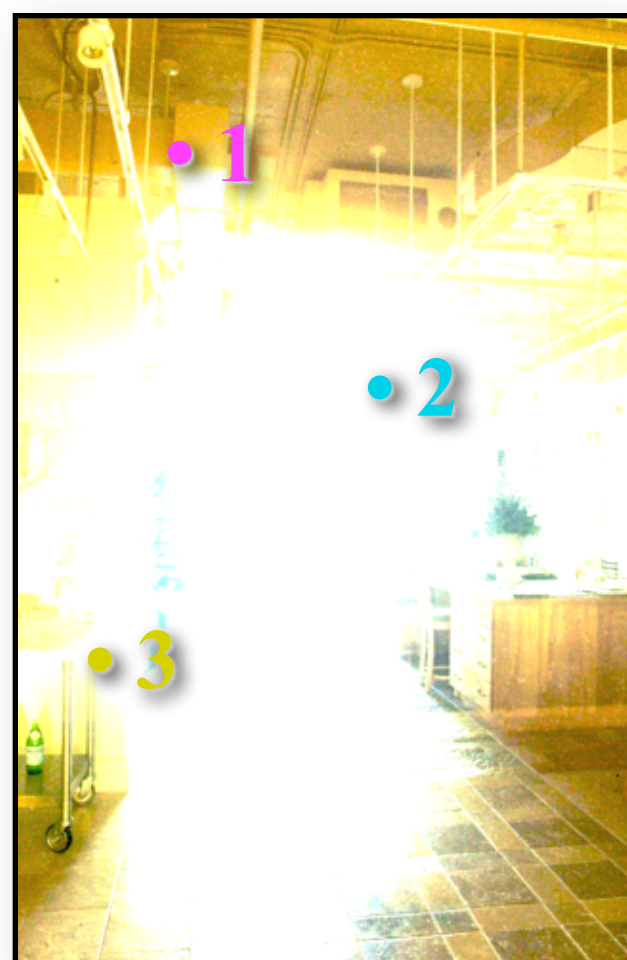




# Optimal Weights

# Problem setup

We may have multiple valid observations for a given pixel  
They have different noise characteristics  
How can we combine them optimally?



# Simple cases

---

They have the same noise

- Just take the average: see assignment 3
- Noise reduced by  $\sqrt{N}$

If one is a lot more noisy?

- Probably focus on the other one
- But if we only use the less noisy one, we don't get any noise reduction
- There has to be a way to use the second one at least a little bit

# Simple case

---

Two observations  $x$  &  $y$  of the same quantity

- with given variances  $\sigma^2[x]$   $\sigma^2[y]$

Compute estimate as  $ax + (1-a)y$

What is the optimal  $a$ ?

# Minimize variance

Variance of the combination:

$$\sigma^2[ax + (1 - a)y] = a^2\sigma^2[x] + (1 - a)^2\sigma^2[y]$$

To minimize: set derivative to zero

$$2a\sigma^2[x] - 2(1 - a)\sigma^2[y] = 0$$

$$a(\sigma^2[x] + \sigma^2[y]) = \sigma^2[y]$$

$$a = \frac{\sigma^2[y]}{\sigma^2[x] + \sigma^2[y]}$$

# Optimal combination

$$\frac{\sigma^2[y]}{\sigma^2[x] + \sigma^2[y]}x + \frac{\sigma^2[x]}{\sigma^2[x] + \sigma^2[y]}y$$

re-arrange:

$$\frac{\sigma^2[x]\sigma^2[y]}{\sigma^2[x] + \sigma^2[y]} \left( \frac{1}{\sigma^2[x]}x + \frac{1}{\sigma^2[y]}y \right)$$

*normalization term*

The optimal combination should scale estimators according to the inverse of their variance



# Verify for same variance

$$\frac{\sigma^2[x]\sigma^2[y]}{\sigma^2[x] + \sigma^2[y]} \left( \frac{1}{\sigma^2[x]}x + \frac{1}{\sigma^2[y]}y \right)$$

# General formula

---

Weight each estimator by the inverse variance

$$\frac{1}{\sum \frac{1}{\sigma^2[x_i]}} \sum \frac{x_i}{\sigma^2[x_i]}$$



# Optimal HDR

# Recall: Assembling HDR (linear case)

Figure out scale factor between images

- from exposure data, or
- by looking at ratios  $I_i(x,y)/I_i(x,y)$  (only when both are good)

Compute weight map  $w_i$  for each image

- binary so far

Reconstruct full image using weighted combination

$$out(x, y) = \frac{1}{\sum w_i(x, y)} \sum w_i(x, y) \frac{1}{k_i} I_i(x, y)$$

# Pixel noise and variance

---

Recall: noise is characterized by its variance

- i.e. each pixel value comes from a true value plus some noise added

We can calibrate this noise by taking multiple exposures, or we can derive variance equations using pen and paper

# Sources of noise

---

## Photon noise

- variance proportional to signal
- dominates for dark pixels

## Read noise

- constant variance
- dominates for dark pixels

**For a pixel value  $x$ :**  $\sigma^2[x] \approx ax + \sigma_{read}^2$

- where  $a$  and  $\sigma_{read}^2$  depend on the camera and ISO

# Optimal weights

Recall irradiance formula:  $I_i(x, y) = \text{clip}(k_i * L(x, y) + n)$

and HDR merging formula:

$$out(x, y) = \frac{1}{\sum w_i(x, y)} \sum w_i(x, y) \frac{1}{k_i} I_i(x, y)$$

1/k amplifies signal and noise:

$$\sigma^2 \left[ \frac{1}{k_i} I_i(x, y) \right] = \frac{1}{k_i^2} \left[ a I_i(x, y) + \sigma_{read}^2 \right]$$

replace I by irradiance

$$\sigma^2 \left[ \frac{1}{k_i} I_i(x, y) \right] = \frac{1}{k_i^2} \left[ a k_i L(x, y) + \sigma_{read}^2 \right]$$

# Variance of one scaled image

$$\sigma^2\left[\frac{1}{k_i}I_i(x, y)\right] = \frac{1}{k_i^2} [aI_i(x, y) + \sigma_{read}^2]$$

$$\sigma^2\left[\frac{1}{k_i}I_i(x, y)\right] = \frac{1}{k_i^2} [ak_iL(x, y) + \sigma_{read}^2]$$

$$\sigma^2\left[\frac{1}{k_i}I_i(x, y)\right] = \frac{a}{k_i}L(x, y) + \frac{1}{k_i^2}\sigma_{read}^2$$

If we only look at photon noise, mostly proportional to scale factor

Ideally, should all be calibrated

Note that we ignored ISO variations



# Improved weight maps

Old formula:  $out(x, y) = \frac{1}{\sum w_i(x, y)} \sum w_i(x, y) \frac{1}{k_i} I_i(x, y)$

Variance per pixel per image:  $\sigma^2[\frac{1}{k_i} I_i(x, y)] \approx \frac{a}{k_i} L(x, y)$

replace  $w_i$  by  $w_i'$

- still use  $w_i$  to reject dark and bright pixels
- but also weight by inverse variance

$$w_i'(x, y) = w_i(x, y) / \frac{a}{k_i} L(x, y)$$

# Improved weight maps

New formula:  $out(x, y) = \frac{1}{\sum w'_i(x, y)} \sum w'_i(x, y) \frac{1}{k_i} I_i(x, y)$

with  $w'_i(x, y) = w_i(x, y) / \frac{a}{k_i} L(x, y)$

Which gives us  $out(x, y) = \frac{1}{\sum w_i(x, y) \frac{k_i}{aL(x, y)}} \sum w_i(x, y) \frac{\cancel{k_i}}{aL(x, y) \cancel{k_i}} \frac{1}{k_i} I_i(x, y)$

- the two  $k_i$  in the main sum cancel each other
- $a$  and  $L(x, y)$  are constant per pixel and present both in the main sum and the normalization. Get rid of them.

$$out(x, y) = \frac{1}{\sum w_i(x, y) k_i} \sum w_i(x, y) I_i(x, y)$$

# New formula

$$out(x, y) = \frac{1}{\sum w_i(x, y) k_i} \sum w_i(x, y) I_i(x, y)$$

The radiant power reaching the pixel has disappeared. All pixels of a given exposure are weighted the same.

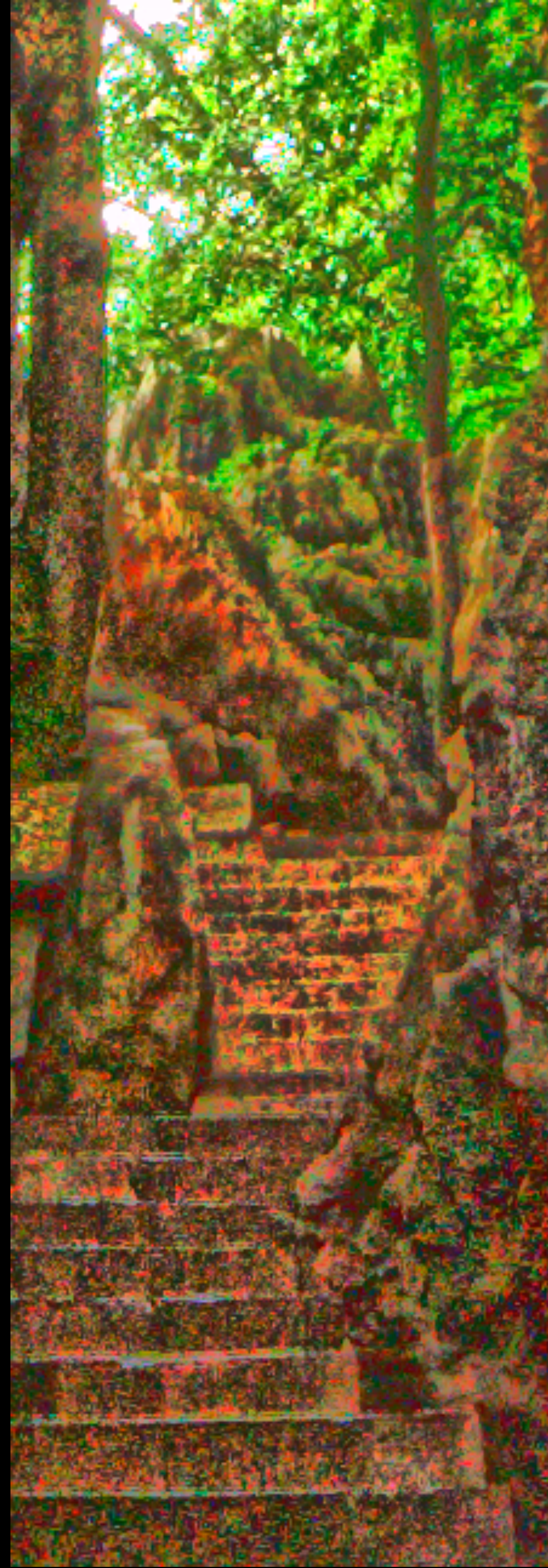
This is because the relative photon noise changes similarly for all pixels between a pair of exposures

- Would be different with read noise

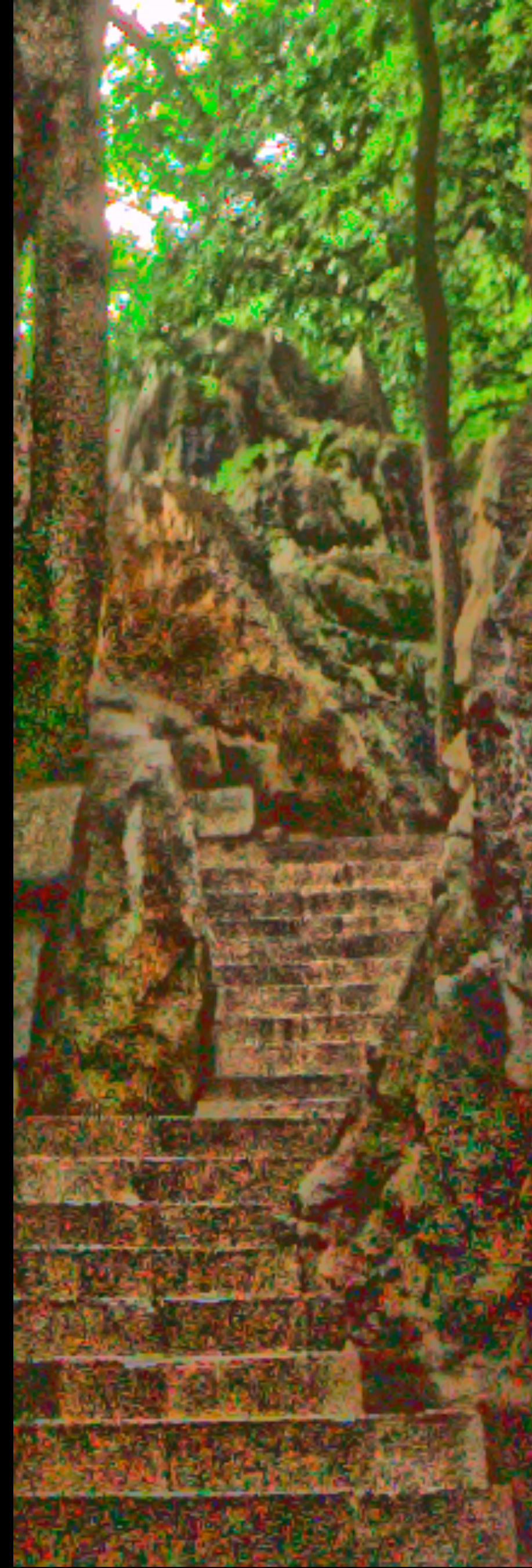
$k_i$  has disappeared from the main sum. The images are not really rescaled to scene radiant power

- But they indirectly are because of the normalization
- Recall that  $k_i$  and  $1/k_i$  used to both appear

After a slide by Frédo Durand



Naive weights



Weighted by  $1/k_i$

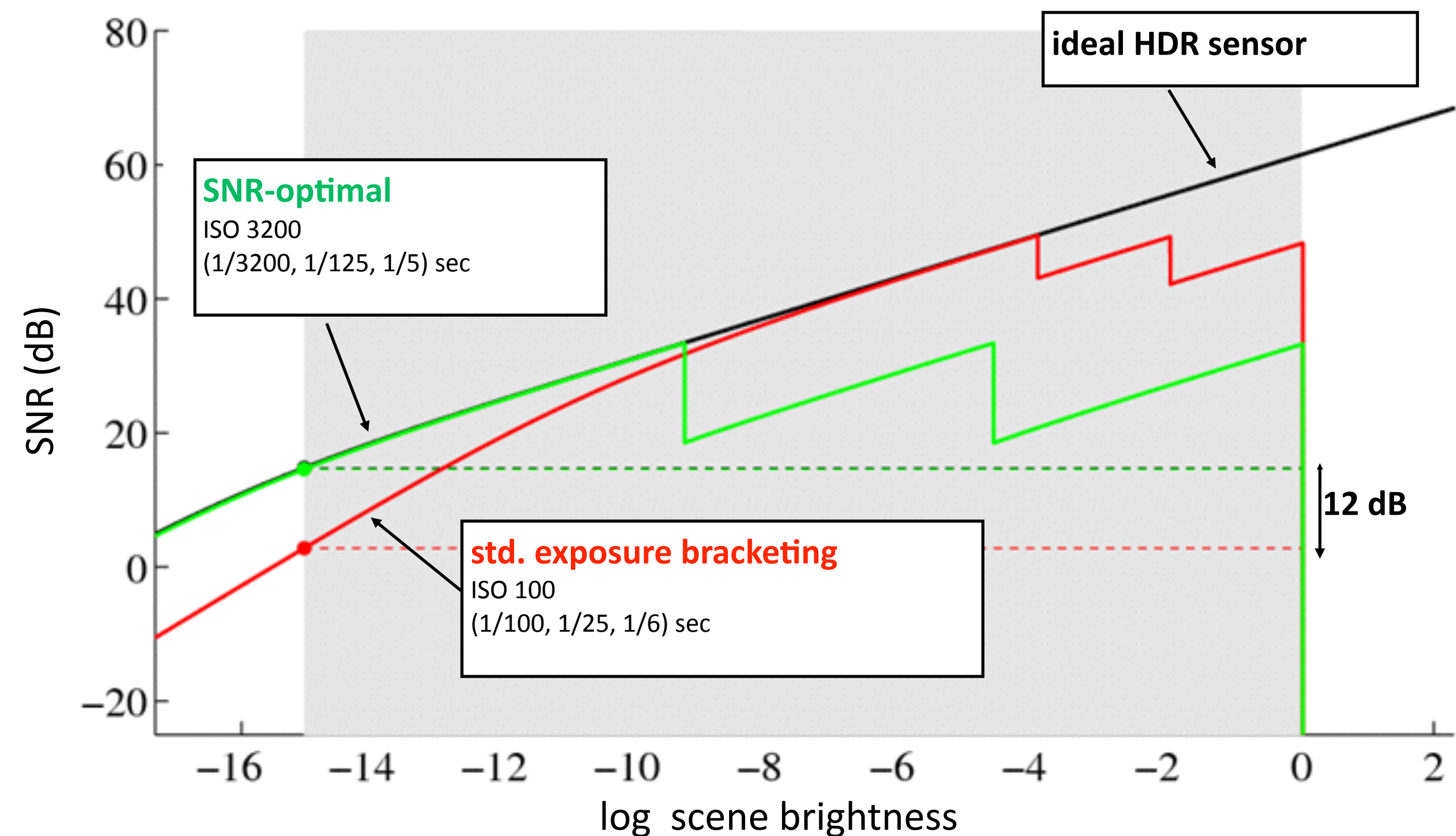


# References

<http://www.macs.hw.ac.uk/bmvc2006/papers/372.pdf>

<http://people.csail.mit.edu/hasinoff/hdrnoise/>

- full noise model
- exploit ISO
- Also optimizes the set of exposures





# HDR file formats

# Storing/Encoding HDR images

Most formats are lossless

**Portable float map (.PFM):**

- straight dump of 32-bit floating-point pixel values
- `fwrite(buffer, 3 * sizeof(float), buffer.size(), f);`
- quick and dirty, common in research

**Radiance image (.PIC, .HDR):**

- 8 bits per r,g,b as usual, plus 8 bits of shared exponent (rgbe)
- Introduced by Greg Ward for Radiance (light simulation)

**Float-point TIFF (.TIFF):**

- log encoded 24- or 32-bit values

**OpenEXR (.EXR):**

- by Industrial Light & Magic, also standard in graphics hardware
- 16- or 32-bit floating-point per channel
- popular in movie industry, not as much in photography

**Adobe Digital NeGative (.DNG)**

- Specific for RAW files, intended to avoid lock-in to undocumented, proprietary formats

# HDR formats

---

Summary of all HDR encoding formats (Greg Ward):

- [http://www.anywhere.com/gward/hdrenc/hdr\\_encodings.html](http://www.anywhere.com/gward/hdrenc/hdr_encodings.html)

Greg's notes:

- <http://www.anywhere.com/gward/pickup/CIC13course.pdf>

<http://www.openexr.com/>

High Dynamic Range Video Encoding (MPI)

- <http://www.mpi-sb.mpg.de/resources/hdrvideo/>





# **HDR photography advice**

# "Good" vs "Bad" HDR/tone mapping

---





# “Good” vs “Bad” HDR/tone mapping

---

Generally avoid:

- halos
- excessive noise
- black clouds
- HDR on people or out-of-focus regions

Not all images require HDR tone mapping!

My opinion: HDR tone mapping is like special effects, it's better if you can't tell it's being used

# How to take your own HDR photos

---

# Keep in mind...

---

HDR + tone mapping/processing won't make a boring photo interesting

Do as much as possible "in-camera"

Learn composition (rule of thirds, line, form, texture, etc)

Shoot in the right light

- golden hour

"Kiliçlar Valley"

[Wojciech Jarosz 2012]



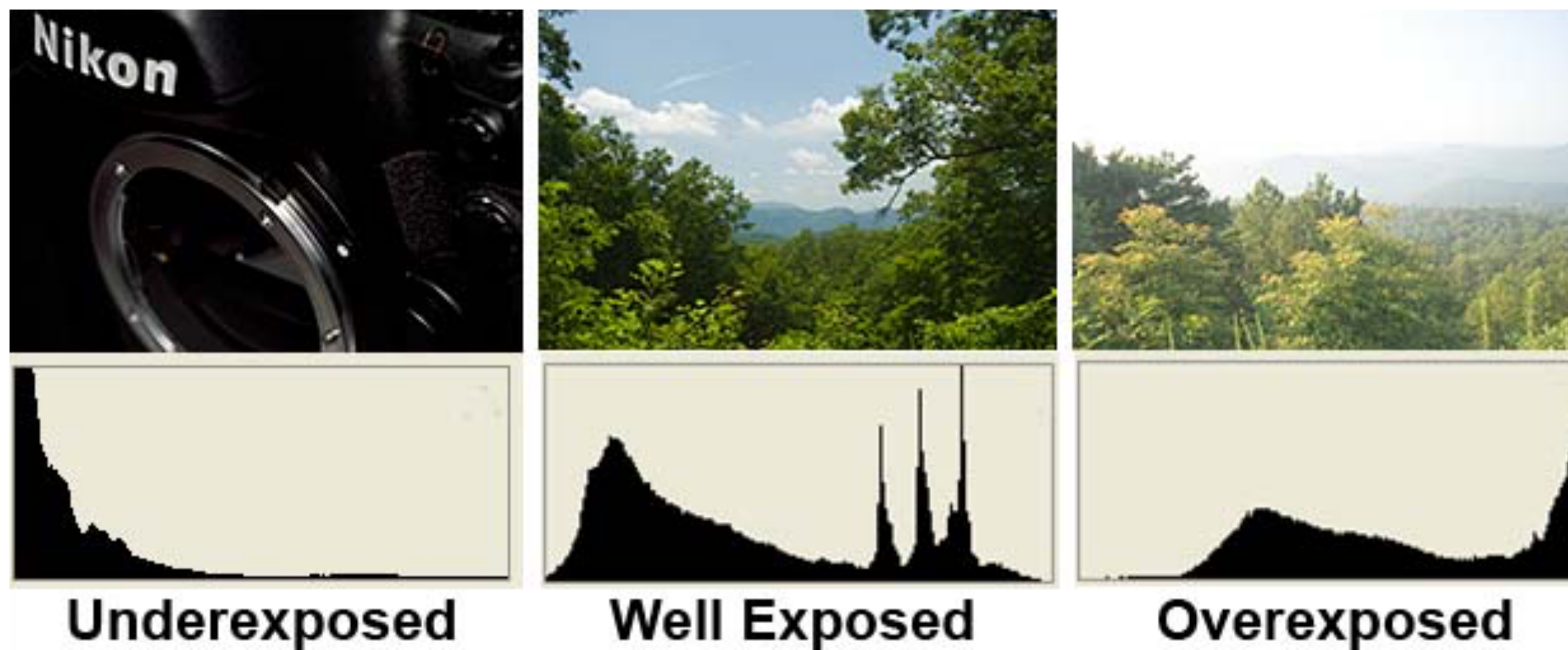




"Kiliçlar Valley"

[Wojciech Jarosz 2012]

# Use the histogram



# What's happening in this photo?



# Polarizing Filter

---



# Polarization



Without Polarizer



With Polarizing Filter

# Polarization



Without Polarizer

With Polarizing Filter

# Effect of Polarization



[Wojciech Jarosz]

# Effect of Polarization



[Wojciech Jarosz]



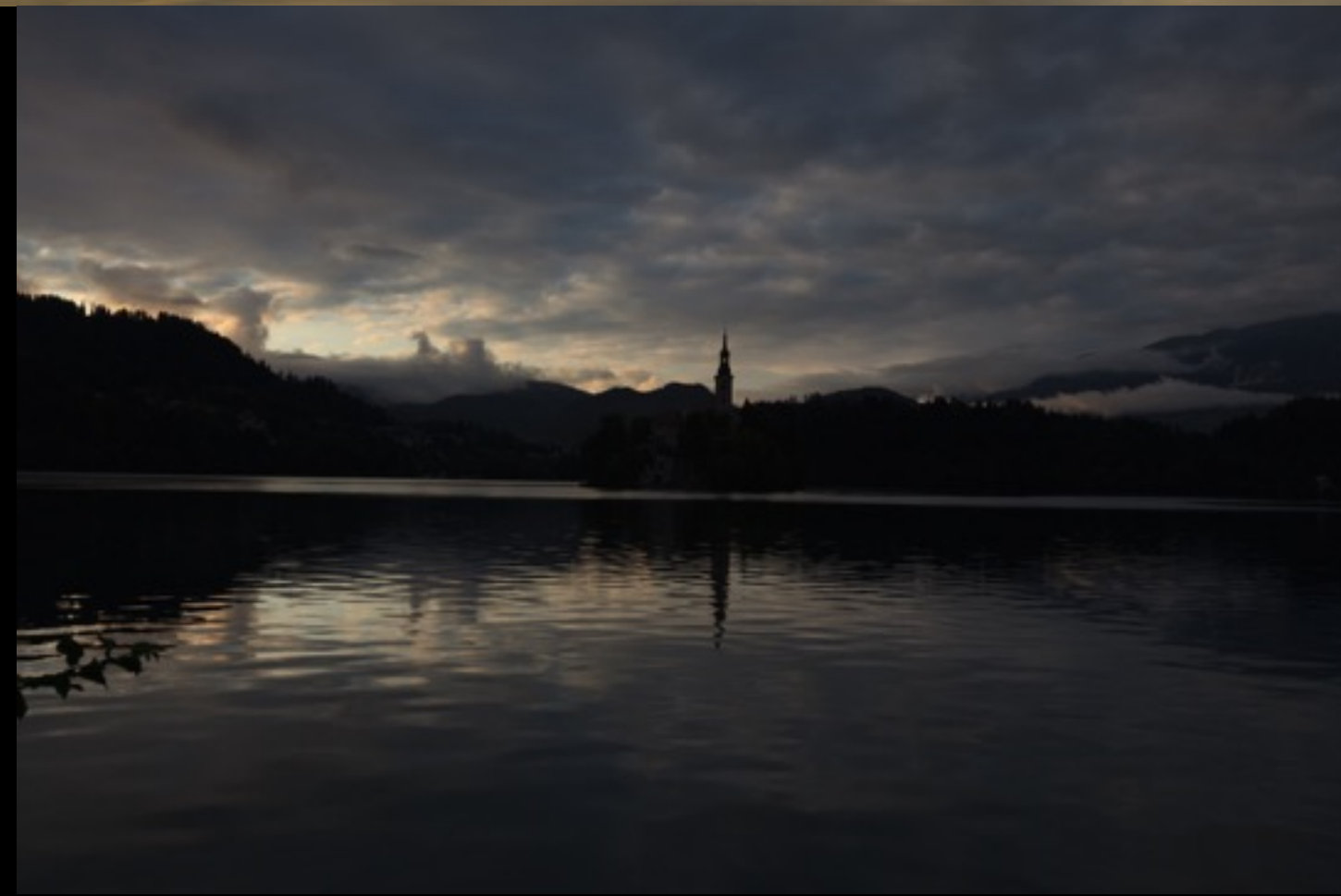
# Exposure Bracketing

---

I typically:

- Use aperture for desired depth of field
- Use lowest possible ISO (reduce noise)
- Control exposure with shutter speed
- Use a tripod **and** a remote trigger (mirror lock-up)





"Lake Bled"

[Wojciech Jarosz 2012]



"La Jolla Hospitals Reef"

[Wojciech Jarosz 2013]



"La Jolla Hospitals Reef"

[Wojciech Jarosz 2013]





# Recap

---

High dynamic range (HDR) imaging is useful, and a new aesthetic

- but is not necessary in all photographic situations

Low dynamic range (LDR) tone mapping methods can also be applied to HDR scenes

- but reducing very HDR scenes to 8 bits for JPEG using only global methods is hard

Local methods reduce large-scale luminance changes (across the image) while preserving local contrast (across edges)

- use edge-preserving filters to avoid halos





# HDR practice

# Slide credits

---

Frédo Durand

Marc Levoy